

S-Plus Instructions

Parametric regression with survreg()

Suppose that you have the following regression model for some continuous, positive random variable T and a vector of explanatory variables (covariates) \mathbf{x} :

$$\ln T = \mathbf{b}_0 + \mathbf{b}'\mathbf{x} + \mathbf{s}W,$$

where W is a continuous random variable on the real line with a distribution that does not involve any unknown parameters. Choices of distributions of T that can be fitted with `survreg()` are extreme value, logistic, gaussian (normal) and Rayleigh, corresponding to, respectively, Weibull, log-logistic, log-normal and log-Rayleigh distribution for T . S-Plus calls $\hat{\alpha}_0$ (Intercept), $\hat{\sigma}$ Dispersion(scale) and the beta's in front of a regressor by the name given to the regressor.

General syntax of survreg()

USAGE:

```
survreg(formula = formula(data), subset, link = c("log"),
        dist = c("extreme", "logistic", "gaussian", "exponential",
                "rayleigh"), fixed = list())
```

ARGUMENTS:

formula: a formula expression as for other regression models. The response is usually a survival object as returned by the `Surv` function. See the documentation for `Surv`, `lm` and `formula` for details.

subset: expression saying that only a subset of the rows of the data should be used in the fit.

link: transformation to be used on the y variable.

dist: assumed distribution for the transformed y variable.

fixed: a list of fixed parameters, most often just the scale.

(Note: there are other optional arguments for survreg() ... see S-Plus help files.)

Example

Let us now fit a log-logistic regression model to the data of Assignment 1, Question 11, assuming no left truncation.

```
> alq11 <- read.table("alq11.dat",header=T)
> alq11.t <- alq11[,1]
> alq11.d <- alq11[,2]
> alq11.x <- as.numeric(alq11[,3]=="D")
> alq11.sr <- survreg(Surv(alq11.t,alq11.d)~alq11.x,dist="logistic")
> alq11.srD <- survreg(Surv(alq11.t[alq11.x==1],alq11.d[alq11.x==1]),
+ dist="logistic")
> alq11.tD <- alq11.t[alq11.x==1]
> alq11.dD <- alq11.d[alq11.x==1]
> alq11.srD <- survreg(Surv(alq11.t[alq11.x==1],alq11.d[alq11.x==1])~1,
+ dist="logistic")
> alq11.srP <- survreg(Surv(alq11.t[alq11.x==0],alq11.d[alq11.x==0])~1,
+ dist="logistic")
```

Let us now look at excerpts of the output of `survreg()`

```
> summary(alq11.sr)
```

Coefficients:

	Value	Std. Error	z value	p
(Intercept)	3.312	0.124	26.743	0.000
alq11.x	0.148	0.163	0.908	0.364

Logistic distribution: Dispersion (scale) est = 0.2126292
Degrees of Freedom: 31 Total; 28 Residual
-2*Log-Likelihood: 21.4

```
> summary(alq11.srD)
```

Coefficients:

	Value	Std. Error	z value	p
(Intercept)	3.46	0.113	30.5	0

Logistic distribution: Dispersion (scale) est = 0.2247572
Degrees of Freedom: 17 Total; 15 Residual
-2*Log-Likelihood: 12.8

```
> summary(alq11.srP)
```

Coefficients:

	Value	Std. Error	z value	p
(Intercept)	3.3	0.121	27.3	0

Logistic distribution: Dispersion (scale) est = 0.1956445
Degrees of Freedom: 14 Total; 12 Residual
-2*Log-Likelihood: 8.41

If we wish to test whether it is reasonable to assume that the scale parameter does not depend on the value of the covariate, we simply fit a model with two different scale parameters (2nd and 3rd `survreg()`) and one model with a common scale parameter (the 1st `survreg()`) and we test if the model reduction is appropriate using a likelihood ratio test. Here, the likelihood ratio statistic is $21.4 - (12.8 + 8.41) = 0.19$, for a p-value of 0.66.