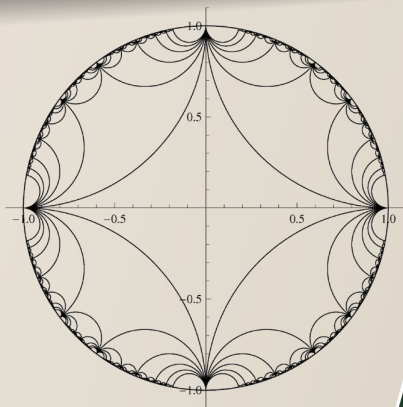


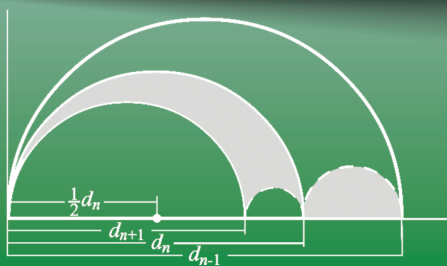
# Basic Complex Analysis

A Comprehensive Course in Analysis, Part 2A

Barry Simon



$$f(z_0) = \frac{1}{2\pi i} \int_{|z|=1} \frac{f(z)}{z - z_0} dz$$



# **Basic Complex Analysis**

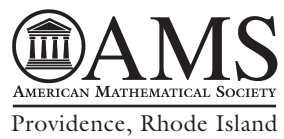
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Barry Simon



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Secondary 34-01, 41-01, 44-01.

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*To the memory of Cherie Galvez  
extraordinary secretary, talented helper, caring person*

*and to the memory of my mentors,  
Ed Nelson (1932-2014) and Arthur Wightman (1922-2013)*

*who not only taught me Mathematics  
but taught me how to be a mathematician*



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# Preface to the Series

Young men should prove theorems, old men should write books.

—Freeman Dyson, quoting G. H. Hardy<sup>1</sup>

Reed–Simon<sup>2</sup> starts with “Mathematics has its roots in numerology, geometry, and physics.” This puts into context the division of mathematics into algebra, geometry/topology, and analysis. There are, of course, other areas of mathematics, and a division between parts of mathematics can be artificial. But almost universally, we require our graduate students to take courses in these three areas.

This five-volume series began and, to some extent, remains a set of texts for a basic graduate analysis course. In part it reflects Caltech’s three-terms-per-year schedule and the actual courses I’ve taught in the past. Much of the contents of Parts 1 and 2 (Part 2 is in two volumes, Part 2A and Part 2B) are common to virtually all such courses: point set topology, measure spaces, Hilbert and Banach spaces, distribution theory, and the Fourier transform, complex analysis including the Riemann mapping and Hadamard product theorems. Parts 3 and 4 are made up of material that you’ll find in some, but not all, courses—on the one hand, Part 3 on maximal functions and  $H^p$ -spaces; on the other hand, Part 4 on the spectral theorem for bounded self-adjoint operators on a Hilbert space and det and trace, again for Hilbert space operators. Parts 3 and 4 reflect the two halves of the third term of Caltech’s course.

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<sup>1</sup>Interview with D. J. Albers, *The College Mathematics Journal*, **25**, no. 1, January 1994.

<sup>2</sup>M. Reed and B. Simon, *Methods of Modern Mathematical Physics, I: Functional Analysis*, Academic Press, New York, 1972.

While there is, of course, overlap between these books and other texts, there are some places where we differ, at least from many:

- (a) By having a unified approach to both real and complex analysis, we are able to use notions like contour integrals as Stieltjes integrals that cross the barrier.
- (b) We include some topics that are not standard, although I am surprised they are not. For example, while discussing maximal functions, I present Garcia's proof of the maximal (and so, Birkhoff) ergodic theorem.
- (c) These books are written to be keepers—the idea is that, for many students, this may be the last analysis course they take, so I've tried to write in a way that these books will be useful as a reference. For this reason, I've included “bonus” chapters and sections—material that I do not expect to be included in the course. This has several advantages. First, in a slightly longer course, the instructor has an option of extra topics to include. Second, there is some flexibility—for an instructor who can't imagine a complex analysis course without a proof of the prime number theorem, it is possible to replace all or part of the (non-bonus) chapter on elliptic functions with the last four sections of the bonus chapter on analytic number theory. Third, it is certainly possible to take all the material in, say, Part 2, to turn it into a two-term course. Most importantly, the bonus material is there for the reader to peruse long after the formal course is over.
- (d) I have long collected “best” proofs and over the years learned a number of ones that are not the standard textbook proofs. In this regard, modern technology has been a boon. Thanks to Google books and the Caltech library, I've been able to discover some proofs that I hadn't learned before. Examples of things that I'm especially fond of are Bernstein polynomials to get the classical Weierstrass approximation theorem, von Neumann's proof of the Lebesgue decomposition and Radon–Nikodym theorems, the Hermite expansion treatment of Fourier transform, Landau's proof of the Hadamard factorization theorem, Wielandt's theorem on the functional equation for  $\Gamma(z)$ , and Newman's proof of the prime number theorem. Each of these appears in at least some monographs, but they are not nearly as widespread as they deserve to be.
- (e) I've tried to distinguish between central results and interesting asides and to indicate when an interesting aside is going to come up again later. In particular, all chapters, except those on preliminaries, have a listing of “Big Notions and Theorems” at their start. I wish that this attempt to differentiate between the essential and the less essential

didn't make this book different, but alas, too many texts are monotone listings of theorems and proofs.

- (f) I've included copious "Notes and Historical Remarks" at the end of each section. These notes illuminate and extend, and they (and the Problems) allow us to cover more material than would otherwise be possible. The history is there to enliven the discussion and to emphasize to students that mathematicians are real people and that "may you live in interesting times" is truly a curse. Any discussion of the history of real analysis is depressing because of the number of lives ended by the Nazis. Any discussion of nineteenth-century mathematics makes one appreciate medical progress, contemplating Abel, Riemann, and Stieltjes. I feel knowing that Picard was Hermite's son-in-law spices up the study of his theorem.

On the subject of history, there are three cautions. First, I am not a professional historian and almost none of the history discussed here is based on original sources. I have relied at times—horrors!—on information on the Internet. I have tried for accuracy but I'm sure there are errors, some that would make a real historian wince.

A second caution concerns looking at the history assuming the mathematics we now know. Especially when concepts are new, they may be poorly understood or viewed from a perspective quite different from the one here. Looking at the wonderful history of nineteenth-century complex analysis by Bottazzini–Grey<sup>3</sup> will illustrate this more clearly than these brief notes can.

The third caution concerns naming theorems. Here, the reader needs to bear in mind Arnol'd's principle:<sup>4</sup> *If a notion bears a personal name, then that name is not the name of the discoverer* (and the related Berry principle: *The Arnol'd principle is applicable to itself*). To see the applicability of Berry's principle, I note that in the wider world, Arnol'd's principle is called "Stigler's law of eponymy." Stigler<sup>5</sup> named this in 1980, pointing out it was really discovered by Merton. In 1972, Kennedy<sup>6</sup> named Boyer's law *Mathematical formulas and theorems are usually not named after their original discoverers* after Boyer's book.<sup>7</sup> Already in 1956, Newman<sup>8</sup> quoted the early twentieth-century philosopher and logician A. N. Whitehead as saying: "Everything of importance has been said before by somebody who

<sup>3</sup>U. Bottazzini and J. Gray, *Hidden Harmony—Geometric Fantasies. The Rise of Complex Function Theory*, Springer, New York, 2013.

<sup>4</sup>V. I. Arnol'd, *On teaching mathematics*, available online at <http://pauli.uni-muenster.de/~munsteg/arnold.html>.

<sup>5</sup>S. M. Stigler, *Stigler's law of eponymy*, *Trans. New York Acad. Sci.* **39** (1980), 147–158.

<sup>6</sup>H. C. Kennedy, *Classroom notes: Who discovered Boyer's law?*, *Amer. Math. Monthly* **79** (1972), 66–67.

<sup>7</sup>C. B. Boyer, *A History of Mathematics*, Wiley, New York, 1968.

<sup>8</sup>J. R. Newman, *The World of Mathematics*, Simon & Schuster, New York, 1956.

did not discover it.” The main reason to give a name to a theorem is to have a convenient way to refer to that theorem. I usually try to follow common usage (even when I know Arnol’d’s principle applies).

I have resisted the temptation of some text writers to rename things to set the record straight. For example, there is a small group who have attempted to replace “WKB approximation” by “Liouville–Green approximation”, with valid historical justification (see the Notes to Section 15.5 of Part 2B). But if I gave a talk and said I was about to use the Liouville–Green approximation, I’d get blank stares from many who would instantly know what I meant by the WKB approximation. And, of course, those who try to change the name also know what WKB is! Names are mainly for shorthand, not history.

These books have a wide variety of problems, in line with a multiplicity of uses. The serious reader should at least skim them since there is often interesting supplementary material covered there.

Similarly, these books have a much larger bibliography than is standard, partly because of the historical references (many of which are available online and a pleasure to read) and partly because the Notes introduce lots of peripheral topics and places for further reading. But the reader shouldn’t consider for a moment that these are intended to be comprehensive—that would be impossible in a subject as broad as that considered in these volumes.

These books differ from many modern texts by focusing a little more on special functions than is standard. In much of the nineteenth century, the theory of special functions was considered a central pillar of analysis. They are now out of favor—too much so—although one can see some signs of the pendulum swinging back. They are still mainly peripheral but appear often in Part 2 and a few times in Parts 1, 3, and 4.

These books are intended for a second course in analysis, but in most places, it is really previous exposure being helpful rather than required. Beyond the basic calculus, the one topic that the reader is expected to have seen is metric space theory and the construction of the reals as completion of the rationals (or by some other means, such as Dedekind cuts).

Initially, I picked “A Course in Analysis” as the title for this series as an homage to Goursat’s *Cours d’Analyse*,<sup>9</sup> a classic text (also translated into English) of the early twentieth century (a literal translation would be

---

<sup>9</sup>E. Goursat, *A Course in Mathematical Analysis: Vol. 1: Derivatives and Differentials, Definite Integrals, Expansion in Series, Applications to Geometry. Vol. 2, Part 1: Functions of a Complex Variable. Vol. 2, Part 2: Differential Equations. Vol. 3, Part 1: Variation of Solutions. Partial Differential Equations of the Second Order. Vol. 3, Part 2: Integral Equations. Calculus of Variations*, Dover Publications, New York, 1959 and 1964; French original, 1905.

“of Analysis” but “in” sounds better). As I studied the history, I learned that this was a standard French title, especially associated with *École Polytechnique*. There are nineteenth-century versions by Cauchy and Jordan and twentieth-century versions by de la Vallée Poussin and Choquet. So this is a well-used title. The publisher suggested adding “Comprehensive”, which seems appropriate.

It is a pleasure to thank many people who helped improve these texts. About 80% was  $\text{\TeX}$ ed by my superb secretary of almost 25 years, Cherie Galvez. Cherie was an extraordinary person—the secret weapon to my productivity. Not only was she technically strong and able to keep my tasks organized but also her people skills made coping with bureaucracy of all kinds easier. She managed to wind up a confidant and counselor for many of Caltech’s mathematics students. Unfortunately, in May 2012, she was diagnosed with lung cancer, which she and chemotherapy valiantly fought. In July 2013, she passed away. I am dedicating these books to her memory.

During the second half of the preparation of this series of books, we also lost Arthur Wightman and Ed Nelson. Arthur was my advisor and was responsible for the topic of my first major paper—perturbation theory for the anharmonic oscillator. Ed had an enormous influence on me, both via the techniques I use and in how I approach being a mathematician. In particular, he taught me all about closed quadratic forms, motivating the methodology of my thesis. I am also dedicating these works to their memory.

After Cherie entered hospice, Sergei Gel’fand, the AMS publisher, helped me find Alice Peters to complete the  $\text{\TeX}$ ing of the manuscript. Her experience in mathematical publishing (she is the “A” of A K Peters Publishing) meant she did much more, for which I am grateful.

This set of books has about 150 figures which I think considerably add to their usefulness. About half were produced by Mamikon Mnatsakanian, a talented astrophysicist and wizard with Adobe Illustrator. The other half, mainly function plots, were produced by my former Ph.D. student and teacher extraordinaire Mihai Stoiciu (used with permission) using *Mathematica*. There are a few additional figures from Wikipedia (mainly under WikiCommons license) and a hyperbolic tiling of Douglas Dunham, used with permission. I appreciate the help I got with these figures.

Over the five-year period that I wrote this book and, in particular, during its beta-testing as a text in over a half-dozen institutions, I received feedback and corrections from many people. In particular, I should like to thank (with apologies to those who were inadvertently left off): Tom Alberts, Michael Barany, Jacob Christiansen, Percy Deift, Tal Einav, German Enciso, Alexander Eremenko, Rupert Frank, Fritz Gesztesy, Jeremy Gray,



Leonard Gross, Chris Heil, Mourad Ismail, Svetlana Jitomirskaya, Bill Johnson, Rowan Killip, John Klauder, Seung Yeop Lee, Milivoje Lukic, Andre Martinez-Finkelshtein, Chris Marx, Alex Poltoratski, Eric Rains, Lorenzo Sadun, Ed Saff, Misha Sodin, Dan Stroock, Benji Weiss, Valentin Zagreb-nov, and Maxim Zinchenko.

Much of these books was written at the tables of the Hebrew University Mathematics Library. I'd like to thank Yoram Last for his invitation and Naavah Levin for the hospitality of the library and for her invaluable help.

This series has a Facebook page. I welcome feedback, questions, and comments. The page is at [www.facebook.com/simon.analysis](http://www.facebook.com/simon.analysis).

Even if these books have later editions, I will try to keep theorem and equation numbers constant in case readers use them in their papers.

Finally, analysis is a wonderful and beautiful subject. I hope the reader has as much fun using these books as I had writing them.

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# Preface to Part 2

Part 2 of this five-volume series is devoted to complex analysis. We've split Part 2 into two pieces (Part 2A and Part 2B), partly because of the total length of the current material, but also because of the fact that we've left out several topics and so Part 2B has some room for expansion. To indicate the view that these two volumes are two halves of one part, chapter numbers are cumulative. Chapters 1–11 are in Part 2A, and Part 2B starts with Chapter 12.

The flavor of Part 2 is quite different from Part 1—abstract spaces are less central (although hardly absent)—the content is more classical and more geometrical. The classical flavor is understandable. Most of the material in this part dates from 1820–1895, while Parts 1, 3, and 4 largely date from 1885–1940.

While real analysis has important figures, especially F. Riesz, it is hard to single out a small number of “fathers.” On the other hand, it is clear that the founding fathers of complex analysis are Cauchy, Weierstrass, and Riemann. It is useful to associate each of these three with separate threads which weave together to the amazing tapestry of this volume. While useful, it is a bit of an exaggeration in that one can identify some of the other threads in the work of each of them. That said, they clearly did have distinct focuses, and it is useful to separate the three points of view.

To Cauchy, the central aspect is the differential and integral calculus of complex-valued functions of a complex variable. Here the fundamentals are the Cauchy integral theorem and Cauchy integral formula. These are the basics behind Chapters 2–5.

For Weierstrass, sums and products and especially power series are the central object. These appear first peeking through in the Cauchy chapters (especially Section 2.3) and dominate in Chapters 6, 9, 10, and parts of Chapter 11, Chapter 13, and Chapter 14.

For Riemann, it is the view as conformal maps and associated geometry. The central chapters for this are Chapters 7, 8, and 12, but also parts of Chapters 10 and 11.

In fact, these three strands recur all over and are interrelated, but it is useful to bear in mind the three points of view.

I've made the decision to restrict some results to  $C^1$  or piecewise  $C^1$  curves—for example, we only prove the Jordan curve theorem for that case.

We don't discuss, in this part, boundary values of analytic functions in the unit disk, especially the theory of the Hardy spaces,  $H^p(\mathbb{D})$ . This is a topic in Part 3. Potential theory has important links to complex analysis, but we've also put it in Part 3 because of the close connection to harmonic functions.

Unlike real analysis, where some basic courses might leave out point set topology or distribution theory, there has been for over 100 years an acknowledged common core of any complex analysis text: the Cauchy integral theorem and its consequences (Chapters 2 and 3), some discussion of harmonic functions on  $\mathbb{R}^2$  and of the calculation of indefinite integrals (Chapter 5), some discussion of fractional linear transformations and of conformal maps (Chapters 7 and 8). It is also common to discuss at least Weierstrass product formulas (Chapter 9) and Montel's and/or Vitali's theorems (Chapter 6).

I also feel strongly that global analytic functions belong in a basic course. There are several topics that will be in one or another course, notably the Hadamard product formula (Chapter 9), elliptic functions (Chapter 10), analytic number theory (Chapter 13), and some combination of hypergeometric functions (Chapter 14) and asymptotics (Chapter 15). Nevanlinna theory (Chapter 17) and univalent functions (Chapter 16) are almost always in advanced courses. The break between Parts 2A and 2B is based mainly on what material is covered in Caltech's course, but the material is an integrated whole. I think it unfortunate that asymptotics doesn't seem to have made the cut in courses for pure mathematicians (although the material in Chapters 14 and 15 will be in complex variable courses for applied mathematicians).



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# Symbol Index

- $A \cap B$ , intersection, 3  
 $A^c$ , complement, 3  
 $A \cup B$ , union, 3  
 $a \equiv b$ , 3  
 $A \setminus B$ , set difference, 3  
 $\mathbb{A}_{r,R}$ , annulus, 2  
 $A \triangle B$ , symmetric difference, 3  
 $\mathfrak{A}(\Omega)$ , all analytic functions on  $\Omega$ , 228  
 $A^*$ , adjoint, 6  
 $\text{Aut}(\mathcal{S})$ , analytic bijection of  $\mathcal{S}$ , 257  
  
 $B(x, y)$ , beta function, 417  
  
 $\mathbb{C}^\times$ ,  $\mathbb{C} \setminus \{0\}$ , 2  
 $\mathbb{C}(X)$ , family of rational function, 286  
 $\mathbb{C}_+$ , upper half-plane, 2  
 $\mathbb{C}$ , complex numbers, 2  
 $\widehat{\mathbb{C}}$ , Riemann sphere,  $\widehat{\mathbb{C}} \cup \{\infty\}$ , 2  
 $\text{cn}(x, k)$ , Jacobi elliptic function, 531  
 $\mathbb{C}\mathbb{P}[1]$ , complex projective line, 256  
 $\mathbb{C}\mathbb{P}[n]$ , complex dimension- $n$  projective space, 268  
  
 $d \mid n$ , divisor, 3  
 $\mathbb{D}_\delta(z_0)$ , disk of radius  $\delta$  about  $z_0$ , 2  
 $\partial\mathbb{D}$ , unit circle in  $\mathbb{C}$ , 2  
 $\mathbb{D}^\times$ ,  $\mathbb{D} \setminus \{0\}$ , 2  
 $\mathbb{D}$ , unit disk in  $\mathbb{C}$ , 2  
 $\bar{\partial}$ , del bar map, 34  
 $\det(A)$ , determinant, 6  
 $\text{dn}(x, k)$ , Jacobi elliptic function, 531  
  
 $\mathcal{F}$ , fundamental domain for  $\text{SL}(2, \mathbb{Z})$ , 484  
  
 $\hat{f}$ , Fourier transform, 124  
 $\|f\|_K$ ,  $\sup_{z \in K} |f(z)|$ , 228  
 $f_n^\#(r)$ , Fourier series coefficients, 124  
 $\widetilde{\mathcal{F}}$ , fundamental domain for  $\Gamma(2)$ , 488  
  
 $\Gamma(2)$ ,  $\{ \begin{pmatrix} \alpha & \beta \\ \gamma & \delta \end{pmatrix} \mid \alpha, \delta \text{ odd integers; } \beta, \gamma \text{ even integers; } \alpha\delta - \beta\gamma = 1 \}$ , 325  
 $\Gamma(T(M))$ , vector fields, 14  
 $\Gamma(z)$ , gamma function, 410  
 $\Gamma_{jk}^i$ , Christoffel symbol, 19  
 $\Gamma(T^*(M))$ , one forms, 15  
 $g_{ij}$ , metric tensor, 18  
  
 $\mathbb{H}_+$ , right half-plane, 2  
 $H_1(X)$ , homology group, 25  
  
 $\text{ins}(\Gamma)$ , inside of  $\Gamma$ , 143  
  
 $\mathcal{J}_{\tau_1, \tau_2}$ , complex torus, 259  
  
 $\mathbf{K}_{j=1}^\infty b_j/a_j$ , continued fraction, 295  
  
 $\log(z)$ , natural logarithm, 2  
 $\mathcal{L}_{\tau_1, \tau_2}$ , lattice generated by  $\tau_1$  and  $\tau_2$ , 258  
  
 $\mathcal{M}(\Omega)$ , functions meromorphic in  $\Omega$ , 249  
  
 $\mathbb{N}$ , natural numbers, 2  
  
 $\text{out}(\Gamma)$ , outside of  $\Gamma$ , 143  
  
 $\pi_1(X, x)$ , fundamental group, 22  
 $\mathbb{P}\text{SL}(2, \mathbb{C})$ , set of FLTs, 275

- $\mathbb{Q}$ , rational numbers, 2
- $\mathbb{R}^\times$ ,  $\mathbb{R} \setminus \{0\}$ , 2
- $\mathbb{R}$ , real numbers, 2
- $\text{Ran } f$ , range of a function  $f$ , 2
- $\upharpoonright$ , restriction, 3
- $S_{\alpha,\beta}$ , sector, 2
- $\sharp(A)$ , number of elements in  $A$ , 2
- $\text{SL}(2, \mathbb{Z})$ ,  $2 \times 2$  matrices with integer elements and determinant 1, 482
- $\text{sn}(x, k)$ , Jacobi elliptic function, 531
- $\text{SO}(3)$ ,  $3 \times 3$  orthogonal matrices, 286
- $\text{SU}(2)$ ,  $2 \times 2$  unitary matrices, 286
- $T(M)$ , tangent bundle, 14
- $T^*(M)$ , cotangent bundle, 14
- $T_{x_0}(M)$ , tangent space to a manifold, 13
- $T_x(M)^*$ , cotangent space, 14
- $\{x\}$ , fractional part of  $x$ , 2
- $[x]$ , greatest integer less than  $x$ , 2
- $\mathbb{Z}_+$ , strictly positive integers, 2
- $\mathbb{Z}$ , integers, 2
- $\mathbb{Z}_k$ , conjugacy classes, 3
- $\mathbb{Z}_k^\times$ , invertible conjugacy classes, 3

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# Subject Index

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