# Sources

Advanced FLUKA Course

# Overview

1. Built-in sources

- Beam definition
- Extended sources
- Colliding beams and synchrotron radiation (SPECSOUR)

2. User-defined sources

- User routine SOURCE
- Useful auxiliary routines
- Sampling techniques
- Two-step methods

3. Example: point vs. extended source

# Built-in sources

# Beam definition – 1

Input card: BEAM

defines several *beam characteristics*:
type of particle, energy, divergence, profile

*Example*

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAM                 3.5 -0.082425       -1.7       0.0       0.0       0.0PROTON
```

- 3.5 GeV/c [**WHAT(1)**] proton beam [**SDUM**] with weight 1 [**WHAT(6)**]
- Gaussian momentum distribution: 0.082425 GeV/c FWHM [**WHAT(2)**]
- Gaussian angular distribution: 1.7 mrad FWHM [**WHAT(3)**]
- no beam width along x (point-like source) [**WHAT(4)**]
- no beam width along y (point-like source) [**WHAT(5)**]

# Beam definition - 2

Input card: BEAMPOS

If **SDUM** = blank:

defines the coordinates of the centre of the beam spot and the beam direction

*Example*

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMPOS          0.0       0.0      -0.1       0.0       0.0       0.0
```

- x-coordinate: 0.0 [**WHAT(1)**]
- y-coordinate: 0.0 [**WHAT(2)**]
- z-coordinate: -0.1 cm [**WHAT(3)**]
- direction cosine with respect to the x-axis: 0.0 [**WHAT(4)**]
- direction cosine with respect to the y-axis: 0.0 [**WHAT(5)**]
- **WHAT(6)** is not used !

→ beam points in the positive z-direction starting at (0.,0.,-0.1)

# Beam definition - 3

Input card: BEAMAXES

defines the beam reference frame which all parameters defined with BEAM and BEAMPOS refer to (angular divergence, transverse profile, polarization, extended sources)

*Example*

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMAXES         1.0       0.0       0.0       0.0 0.7071068 0.7071068
```

- cosine of angle between x-axis of beam and x-axis of geometry frame [WHAT(1)]
- cosine of angle between x-axis of beam and y-axis of geometry frame [WHAT(2)]
- cosine of angle between x-axis of beam and z-axis of geometry frame [WHAT(3)]

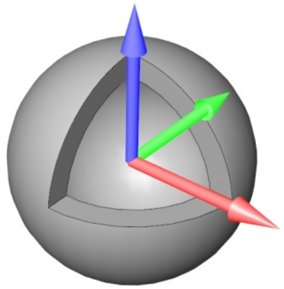
  (1.,0,0) → x-axes of beam and geometry frames are parallel

- cosine of angle between z-axis of beam and x-axis of geometry frame [WHAT(4)]
- cosine of angle between z-axis of beam and y-axis of geometry frame [WHAT(5)]
- cosine of angle between z-axis of beam and z-axis of geometry frame [WHAT(6)]

  (0.,0.7071068,0.7071068) → z-axis of beam frame is at 45deg to both y- and z-axes of geometry frame

# Extended sources - *Spherical shell source*

Input card: BEAMPOS



If **SDUM** = **SPHE-VOL**:

defines a spatially extended source in a spherical shell

*Example*

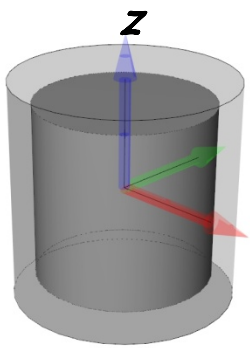
```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMPOS                0.0       0.0       0.0       0.0       0.0       0.0
BEAMPOS                0.0       1.0       0.0       0.0       0.0       0.0SPHE-VOL
```

- radius (in cm) of the inner sphere shell: 0.0 cm [**WHAT(1)**]
- radius (in cm) of the outer sphere shell: 1.0 cm [**WHAT(2)**]
- **WHAT(3)** - **WHAT(6)** are not used !

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards.

# Extended sources – *Cylindrical shell source*

Input card: BEAMPOS




If **SDUM** = **CYLI-VOL**:

defines a spatially extended source in a cylindrical shell with the height parallel to the z-axis of the beam frame

***Example***

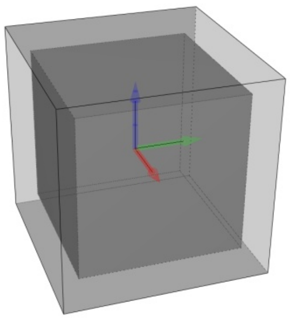
```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMPOS          0.0       0.0       0.0       0.0       0.0       0.0
BEAMPOS          0.0       1.0       0.0       1.0       0.0       0.0CYLI-VOL
```

- radius (in cm) of the inner cylinder defining the shell: 0.0 cm [**WHAT(1)**]
- radius (in cm) of the outer cylinder defining the shell: 1.0 cm [**WHAT(2)**]
- height (in cm) of the inner cylinder defining the shell: 0.0 cm [**WHAT(3)**]
- height (in cm) of the outer cylinder defining the shell: 1.0 cm [**WHAT(4)**]
- **WHAT(5)** - **WHAT(6)** are not used !

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards.

# Extended sources - *Cartesian shell source*

Input card: BEAMPOS



If **SDUM** = **CART-VOL**:
defines a spatially extended source in a Cartesian shell with the sides parallel to the beam frame axes

*Example*

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMPOS          0.0       0.0       0.0       0.0       0.0       0.0
BEAMPOS          0.0       1.0       0.0       1.0       0.0       1.0CART-VOL
```

- length (in cm) of the x-side of the inner parallelepiped defining the shell: 0.0 cm [**WHAT(1)**]
- length (in cm) of the x-side of the outer parallelepiped defining the shell: 1.0 cm [**WHAT(2)**]
- length (in cm) of the y-side of the inner parallelepiped defining the shell: 0.0 cm [**WHAT(3)**]
- length (in cm) of the y-side of the outer parallelepiped defining the shell: 1.0 cm [**WHAT(4)**]
- length (in cm) of the z-side of the inner parallelepiped defining the shell: 0.0 cm [**WHAT(5)**]
- length (in cm) of the z-side of the outer parallelepiped defining the shell: 1.0 cm [**WHAT(6)**]

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards.

# Extended sources – *Spherical surface source*

Input card: BEAMPOS

If **SDUM** = **FLOOD**:

defines a source distribution on a spherical surface

*Example*

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMPOS          0.0       0.0       0.0       0.0       0.0       0.0
BEAMPOS          1.0       0.0       0.0       0.0       0.0       0.0FLOOD
```

- radius (in cm) of the sphere: 1.0 cm [**WHAT(1)**]
- **WHAT(2)** - **WHAT(6)** are not used !

The surface is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction is sampled according to a diffusive distribution so as to generate a uniform fluence equal to $1/(\pi R^2)$ inside the sphere (in absence of materials)

# Extended sources - *Example*

Radioactive source of $^{60}Co$ (two main $\gamma$-emissions: 1332.5 keV and 1173.2 keV)

cylindrical shape, 2cm diameter, 2mm height along z, centre of cylinder base at origin

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAM             0.0                                                ISOTOPE
HI-PROPE        27.0       60.0
BEAMPOS          0.0        0.0        0.1        0.0        0.0        0.0
BEAMPOS          0.0        1.0        0.0        0.2        0.0        0.0CYLI-VOL
```

or

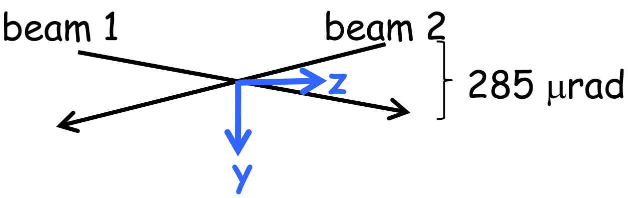
```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAM       1252.8E-6               10000.                               PHOTON
BEAMPOS          0.0        0.0        0.1        0.0        0.0        0.0
BEAMPOS          0.0        1.0        0.0        0.2        0.0        0.0CYLI-VOL
```

If height along x (instead of z) add

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
BEAMAXES         0.0        0.0       -1.0        1.0        0.0        0.0
```

# Special sources – hadron-nucleus *collision*

Input card: SPECSOUR




***Example:*** LHC

7 TeV/c, full crossing angle of 285 μrad in yz-plane

Momentum vectors of colliding beams: *three possibilities*

*1)* If **SDUM** = **PPSOURCE**:

```
SPECSOUR           0.     0.9975 6999.9999         0.0     0.9975-6999.9999PPSOURCE
```

- x, y, z-components of lab momentum for beam 1 particle [WHAT(1-3)]
- x, y, z-components of lab momentum for beam 2 particle [WHAT(4-6)]

*2)* If **SDUM** = **CROSSASY**:

```
SPECSOUR        7000.   142.5E-6       90.0      7000.   142.5E-6         0.0CROSSASY
```

- lab momentum for beam 1 particle [WHAT(1)]
- polar angle (rad) between beam 1 particle momentum and positive z-direction [WHAT(2)]
- azimuth angle (deg!) defining crossing plane [WHAT(3)]
- lab momentum for beam 2 particle [WHAT(4)]
- polar angle (rad) between beam 2 particle momentum and negative z-direction [WHAT(5)]

# Special sources – hadron-nucleus *collision*

3) If SDUM = CROSSSYM:

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
SPECSOUR        7000.   142.5E-6       90.0        0.0        0.0        0.0CROSSSYM
```

- lab momentum for beam 1 and 2 particle [WHAT(1)]
- half crossing angle (rad) [WHAT(2)]
- azimuth angle (deg!) defining crossing plane [WHAT(3)]
- WHAT(4) - WHAT(6) are not used !

Interaction point of colliding beams (continuation card):

```
SPECSOUR        7000.   142.5E-6       90.0        0.0        0.0        0.0CROSSSYM
SPECSOUR       12.E-4     12.E-4        5.0                                  &
```

- sigma_x in cm for Gaussian sampling around XBEAM: 12 um [WHAT(7)]
- sigma_y in cm for Gaussian sampling around YBEAM: 12 um [WHAT(8)]
- sigma_z in cm for Gaussian sampling around ZBEAM: 5 cm [WHAT(9)]

(XBEAM,YBEAM,ZBEAM) defined with BEAMPOS card

- sampling limit, in sigma, applying along x, y, and z [WHAT(10)]

  =< 0 no limit

# Special sources - hadron-nucleus *collision*

```
BEAM            3000.0                                                            HEAVYION
HI-PROPE          82.0      208.0
...
SPECSOUR        574000.   142.5E-6       90.0        0.0        0.0        0.0CROSSSYM
SPECSOUR         12.E-4     12.E-4        5.0                            208.0&
SPECSOUR           82.                                                       &
```

- ID of beam 1 particle (default: the one of BEAM) [WHAT(11)]
- mass number of beam 2 particle (default: proton) [WHAT(12)]
- charge of beam 2 particle [WHAT(13)]

```
SPECSOUR        7000.0   0.000335      180.0        0.0        0.0        0.0CROSSSYM
SPECSOUR           0.0        0.0       5.34        0.0                   0.0&
SPECSOUR           1.0  1.057E-5   1.057E-5   1.057E-5   1.057E-5         0.0&&
```

- sigma_th_C (rad) for the Gaussian sampling of the beam 1 particle angle [WHAT(14)]
  wrt the ideal momentum in the *Crossing* plane
- sigma_th_O (rad) for the Gaussian sampling of the beam 1 particle angle [WHAT(15)]
  wrt the ideal momentum in the *Orthogonal* plane
- the same as WHAT(14) for beam 2 particle [WHAT(16)]
- the same as WHAT(15) for beam 2 particle [WHAT(17)]

# Special sources – hadron-nucleus *collision*

Three interaction types are available:

- i0 + i1 * 10 + i2 * 100 [**WHAT(18)**]

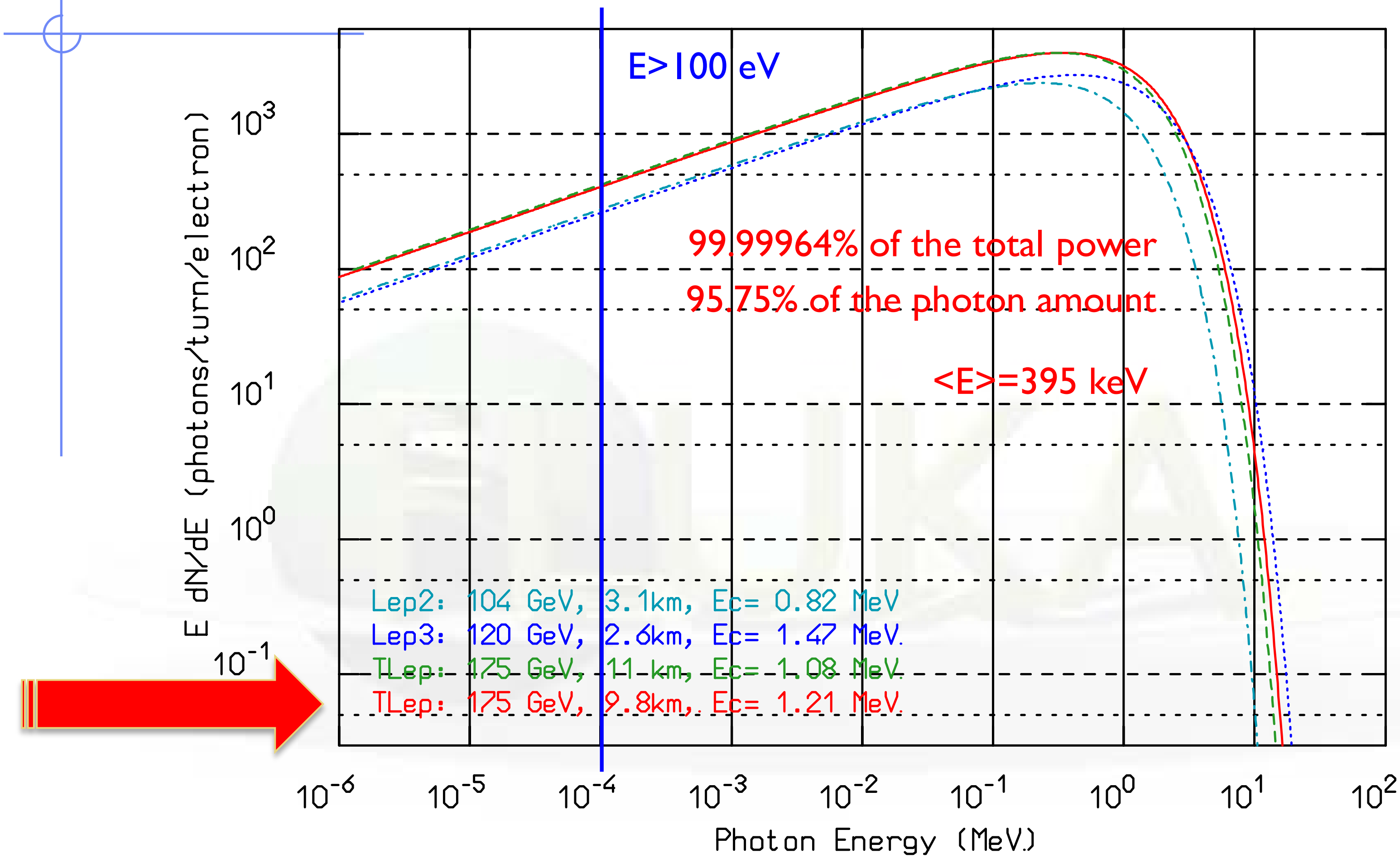
i0 = flag for **nuclear nonelastic** interactions
i1 = flag for **nuclear elastic** interactions
i2 = flag for **electromagnetic dissociation** (EMD) interactions
default: nuclear nonelastic + EMD if selected with the **PHYSICS(SDUM = EM-DISSO)** card

For collisions in the DPMJET energy range, don't forget (to link it as well as to input) the following card

```
*...+....1....+....2....+....3....+....4....+....5....+....6....+....7....+...
PHYSICS       8000.0                                                  LIMITS
```

**WHAT(1)** [GeV/c] must be larger than the maximum nucleon centre-of-mass momentum

# SYNCHROTRON RADIATION



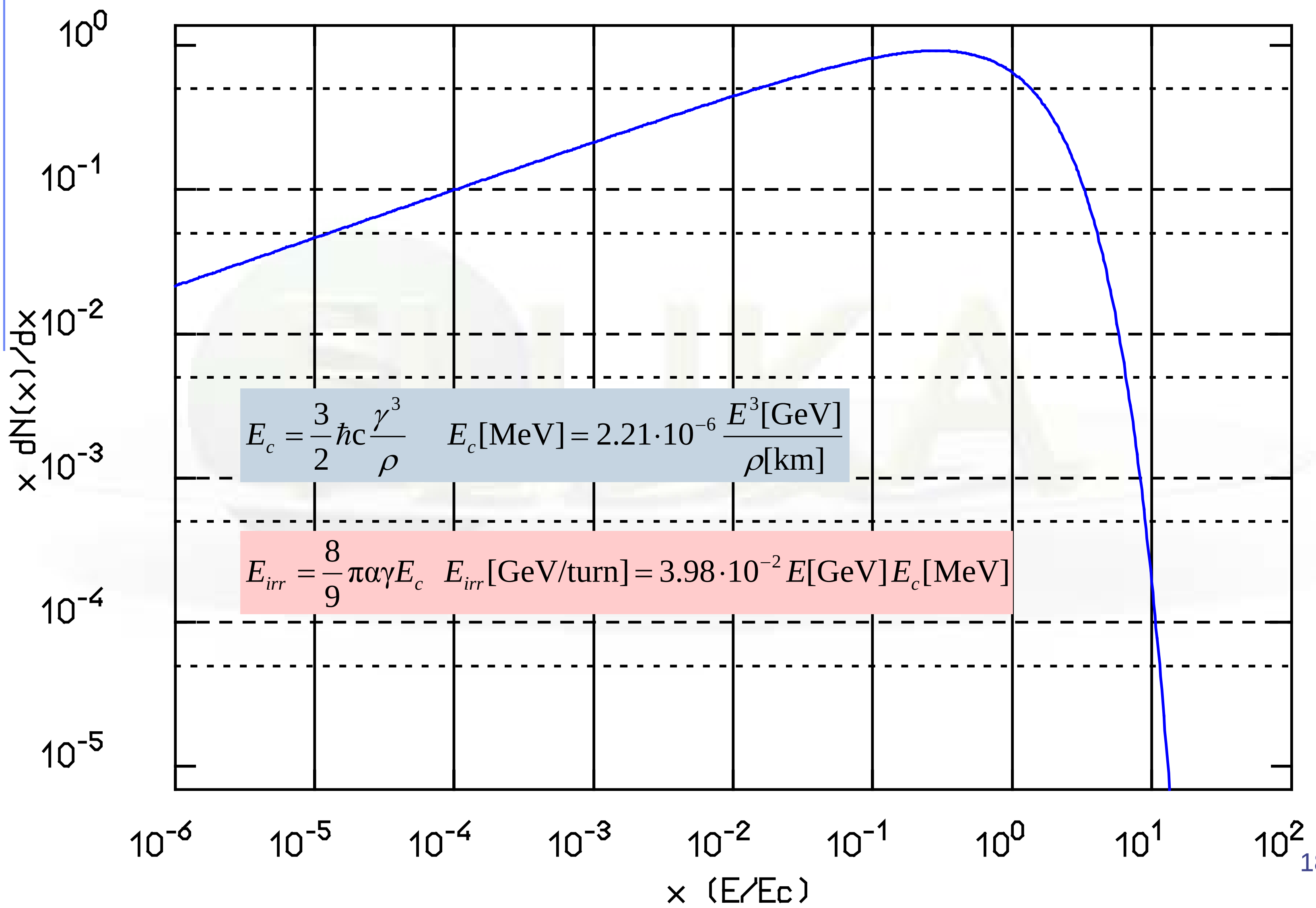

- $\Delta E$= 8.5 GeV/turn (dE/ds=1.375 keV/cm in the dipoles)
- P = 8.5 x I[mA] MW = 8.5 x 10mA = 85 MW in the whole accelerator

  (dP/ds= 1.375 x I[mA] W/cm in the dipoles)

# Special sources – *synchrotron radiation*

- Sophisticated low energy photon transport including polarization effects for Compton, photoelectric and coherent scattering, and full account for bound electron effects: already available in FLUKA since several years
- Now dedicated "generic" source for SR radiation accounting for:
  - ✓ Spectrum sampling
  - ✓ Polarization as a function of emitted photon energy
  - ✓ Angular distribution
  - ✓ Arbitrary orientation emitting particle vs magnetic field
  - ✓ Photon emission along arcs/helical paths

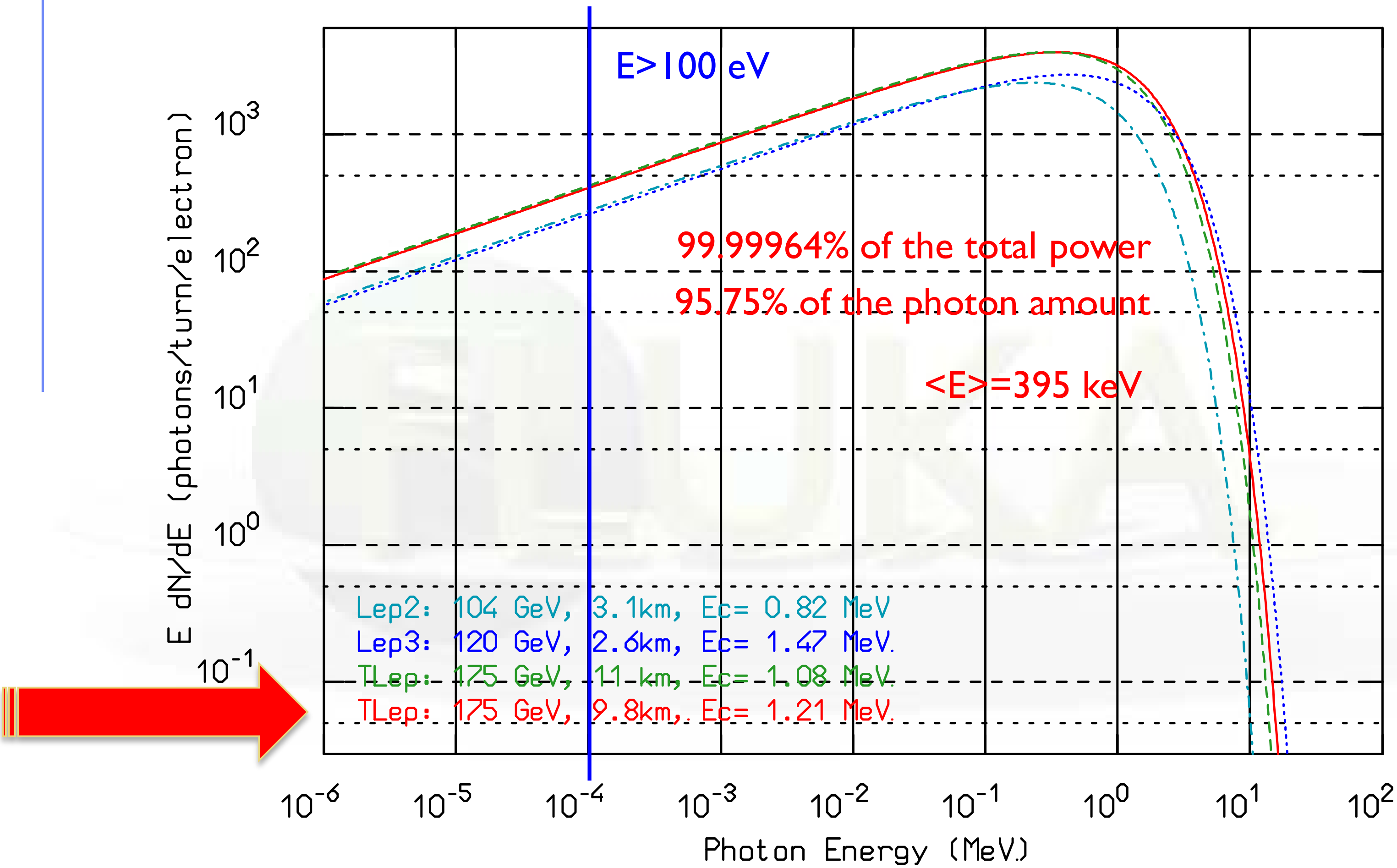
# Special sources – *synchrotron radiation*




$$E_c = \frac{3}{2}\hbar c \frac{\gamma^3}{\rho} \qquad E_c[\text{MeV}] = 2.21\cdot 10^{-6}\,\frac{E^3[\text{GeV}]}{\rho[\text{km}]}$$

$$E_{irr} = \frac{8}{9}\pi\alpha\gamma E_c \quad E_{irr}[\text{GeV/turn}] = 3.98\cdot 10^{-2}\,E[\text{GeV}]\,E_c[\text{MeV}]$$

# Special sources – *synchrotron radiation*




- $\Delta$E= 8.5 GeV/turn (dE/ds=1.375 keV/cm in the dipoles)
- P = 8.5 x I[mA] MW = 8.5 x 10mA = 85 MW in the whole accelerator (dP/ds= 1.375 x I[mA] W/cm in the dipoles)

# Special sources – *synchrotron radiation*

```
FREE
SPECSOUR  , ELECTRON, 175.0, 979948.86, 0.0000001, 0.0, -1.0, SYNC-RAD
SPECSOUR  , 1050.0, -0.59467382951, 0., 1134.9997568, -.10714843289E-02, 0.0, &
FIXED
```

- particle emitting the radiation [WHAT(1)]
- emitting particle momentum [GeV/c if >0] or kinetic energy [GeV if <0] [WHAT(2)]
- curvature radius [cm if >0] or magnetic field [T if <0] [WHAT(3)]
- photon spectrum lower limit [GeV] [WHAT(4)]
- x/y-components of the magnetic field versor [WHAT(5/6)]

  *The z-component sign is positive for SYNC-RAD and negative for SYNC-RDN*

- length [cm] of the emission arc [WHAT(7)]
- coordinates (x/y/z [cm]) of the starting point of a possible second arc of same length [WHAT(8/9/10)]
- x/y-components of the emitting particle direction versor at the beginning of the second arc [WHAT(11/12)]

The starting point of the first arc as well the initial direction of the emitting particle are defined in the BEAMPOS card

# BEAM Visualization

# Within geometry viewer

The beam position and direction can be plotted with arrows inside the flair geometry editor.

- Add a #define to set the beam length
  #define bl 50.0

- Add an !arrow card and set as what's the following functions:

```
x:      =c(BEAMPOS,0,1)
y:      =c(BEAMPOS,0,2)
z:      =c(BEAMPOS,0,3)
dx:     =bl*c(BEAMPOS,0,4)
dy:     =bl*c(BEAMPOS,0,5)
dz:     =bl*sqrt(1.0-c(BEAMPOS,0,4)**2-c(BEAMPOS,0,5)**2)
```

c(BEAMPOS,n,m) is a function that returns from the $n^{th}$ (zero based) BEAMPOS card the $m^{th}$ argument

# USRBIN

- Create a **`USRBIN`** covering the beam position (preferentially Cartesian X-Y-Z) with BEAMPART as scoring particle
- Set all materials to VACUUM (to speed up calculation)
- Make one run of 1 cycle
- Visualize the results:
  - in flair as USRBIN plot
  - in the geometry editor as a custom USRBIN layer (don't forget to set properly the colorband)

# With USERDUMP

- Add a **`USERDUMP`** card selecting ONLY Source particles
- Make one run of 1 cycle
- Create a USERDUMP plot in flair:

  Select the “Source” tab

  You have the ability to make

  - 1D histogram plots of any of the source quantities
  - 2D scattered plots for any of the source quantities with even the possibility to overlay on a geometry image

# User-defined sources

# Source routine - 1

- Allows the definition of primary particle properties (in space, energy, time, direction, or mixture of particles) which cannot be described with built-in sources

- Activated with input card SOURCE. The parameter list of that card (two continuation cards possible!) allows the user to pass on up to 18 numerical values `WHASOU(1-18)`and one 8-character string `SDUSOU` via `COMMON /SOURCM/`

- At each call, one (or more) particle(s) must be loaded onto `COMMON /FLKSTK/` (particle bank) before returning control. The relevant variable values can be read from a file, generated by some sampling algorithm, or just assigned.

- *Argument list*: if `NOMORE=1` (output variable) the run will be terminated after exhausting the primary particles loaded onto the stack in the present call. The history number limit set with card START will be overridden.

# Source routine - 2

```
...
      LOGICAL LFIRST
*
      SAVE LFIRST
      DATA LFIRST / .TRUE. /
...
      NOMORE = 0
*  +-------------------------------------------------------------------*
*  |  First call initializations:
      IF ( LFIRST ) THEN
*  |  *** The following 3 cards are mandatory ***
         LFIRST = .FALSE.
         TKESUM = ZERZER
         LUSSRC = .TRUE.
*  |  *** User initialization ***
```

Any first-time initialization can be inserted here, for example
- setting up parameters passed on via SOURCE card
- reading spectra from data files

```
      END IF
...
```

# Source routine - 3

```
...
      NPFLKA = NPFLKA + 1
* Wt is the weight of the particle
      WTFLK  (NPFLKA) = ONEONE
      WEIPRI = WEIPRI + WTFLK (NPFLKA)
* Particle type (1=proton.....). Ijbeam is the type set by the BEAM
* card
*  +-------------------------------------------------------------------*
*  |  (Radioactive) isotope:
      IF ( IJBEAM .EQ. -2 .AND. LRDBEA ) THEN
         IARES  = IPROA
         IZRES  = IPROZ
         IISRES = IPROM
         CALL STISBM ( IARES, IZRES, IISRES )
         IJHION = IPROZ  * 1000 + IPROA
         IJHION = IJHION * 100 + KXHEAV
         IONID  = IJHION
         CALL DCDION ( IONID )
         CALL SETION ( IONID )
*  |
*  +-------------------------------------------------------------------*
*  |  Heavy ion:
      ELSE IF ( IJBEAM .EQ. -2 ) THEN
         IJHION = IPROZ  * 1000 + IPROA
         IJHION = IJHION * 100 + KXHEAV
         IONID  = IJHION
         CALL DCDION ( IONID )
         CALL SETION ( IONID )
         ILOFLK (NPFLKA) = IJHION
*  |  Flag this is prompt radiation
         LRADDC (NPFLKA) = .FALSE.
*  |  Group number for "low" energy neutrons, set to 0 anyway
         IGROUP (NPFLKA) = 0
*  |
*  +-------------------------------------------------------------------*
*  |  Normal hadron:
      ELSE
         IONID = IJBEAM
         ILOFLK (NPFLKA) = IJBEAM
*  |  Flag this is prompt radiation
         LRADDC (NPFLKA) = .FALSE.
*  |  Group number for "low" energy neutrons, set to 0 anyway
         IGROUP (NPFLKA) = 0
      END IF
*  |
*  +-------------------------------------------------------------------*
...
```

increase pointer in FLKSTK

weight of particle
(if varying -> biased source)

total weight of primaries (don't change)

Definition of particle type

- The template sets the type of particle equal to the one defined by the BEAM card (and HI-PROPE, if used).

- Whichever valid particle type can be set inside the source (may be varying event by event)

# Source routine - 4

```
...
* Particle age (s)
      AGESTK (NPFLKA) = +ZERZER
      AKNSHR (NPFLKA) = -TWOTWO
* Kinetic energy of the particle (GeV)
      TKEFLK (NPFLKA) = SQRT ( PBEAM**2 + AM (IONID)**2 ) - AM (IONID)
* Particle momentum
      PMOFLK (NPFLKA) = PBEAM
* Cosines (tx,ty,tz)
      TXFLK  (NPFLKA) = UBEAM
      TYFLK  (NPFLKA) = VBEAM
      TZFLK  (NPFLKA) = WBEAM
*     TZFLK  (NPFLKA) = SQRT ( ONEONE - TXFLK (NPFLKA)**2
*    &                       - TYFLK (NPFLKA)**2 )
* Polarization cosines:
      TXPOL  (NPFLKA) = -TWOTWO
      TYPOL  (NPFLKA) = +ZERZER
      TZPOL  (NPFLKA) = +ZERZER
* Particle coordinates
      XFLK   (NPFLKA) = XBEAM
      YFLK   (NPFLKA) = YBEAM
      ZFLK   (NPFLKA) = ZBEAM
...
```

momentum and energy
- by default taken from BEAM card (PBEAM in COMMON /BEAMCM/)
- the user can set (consistently!) any momentum or energy here (either from file or sampled)
- **NOTE:** BEAM card is always mandatory for initialization purposes. Momentum/energy set here must not exceed the respective BEAM card value.

direction cosines and coordinates
- by default taken from BEAMPOS card (COMMON /BEAMCM/)
- ensure proper normalization of cosines!

polarization
- TXPOL = -2 flag for "no polarization"

# Source routine - 5

```
* User dependent flag:
      LOUSE  (NPFLKA) = 0
...
* User dependent spare variables:
      DO 100 ISPR = 1, MKBMX1
         SPAREK (ISPR,NPFLKA) = ZERZER
 100  CONTINUE
* User dependent spare flags:
      DO 200 ISPR = 1, MKBMX2
         ISPARK (ISPR,NPFLKA) = 0
 200  CONTINUE
```

Variables that allow to store additional information in `COMMON /FLKSTK/`,
such as information on ancestors of a certain particle

# Auxiliary routines - *Random numbers*

**… = FLRNDM (XDUMMY)**

returns a 64-bit random number [0-1)

**NOTE:** Fundamental for SOURCE! No other external random generators must be used, otherwise the history reproducibility will be lost.

**CALL FLNRRN (RGAUSS)**

returns a normally distributed random number RGAUSS

**CALL FLNRR2 (RGAUS1,RGAUS2)**

returns an uncorrelated pair of normally distributed random numbers RGAUS1 and RGAUS2

**CALL SFECFE (SINT,COST)**

returns SINT and COST, sine and cosine of a random azimuthal angle

SINT**2 + COST**2 = 1.D+00

**CALL RACO (TXX, TYY, TZZ)**

returns a random 3D direction (TXX, TYY, TZZ)

TXX**2 + TYY**2 + TZZ**2 = 1.D+00

# Auxiliary routines – *Name <-> number conv.*

Conversion of region name to number

```
CALL GEON2R ( REGNAM, NREG, IERR )
```

Input variable:

REGNAM = region name (CHARACTER*8)

Output variables:

NREG = region number

IERR = error code (0 on success, 1 on failure)

Conversion of region number to name

```
CALL GEOR2N ( NREG, REGNAM, IERR )
```

Input variable:

NREG = region number

Output variables:

REGNAM = region name (CHARACTER*8)

IERR = error code (0 on success, 1 on failure)

# Auxiliary routines – *Others*

**CALL OAUXFI ('file', LUN, 'CHOPT', IERR)**

to open an auxiliary file (to read data or parameters) looking automatically for the file in some default locations (temporary directory, working directory)

**CALL FLABRT ('routine_name','message')**

this allows to force a FLUKA abort on user request: it might be useful to perform a debugging (using gdb for instance)

**CALL SFLOOD ( XXX, YYY, ZZZ, UXXX, VYYY, WZZZ )**

returns a random position XXX, YYY, ZZZ on the surface of a sphere of radius 1 and centre 0 (multiply XXX, YYY, ZZZ by the actual radius and add the centre coordinates) and a random direction UXXX, VYYY, WZZZ (cosines) so as to generate a uniform fluence inside the sphere, equal to $1/(\pi R^2)$, being R the actual sphere radius.

# Sampling from a distribution – *Discrete*

## 1) From the cumulative distribution

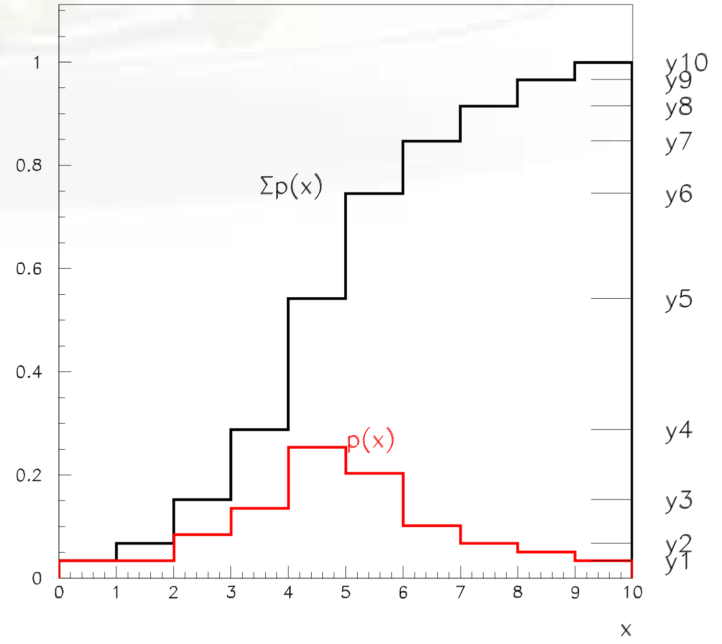
- Suppose to have a *discrete* random variable $x$, that can assume values $x_1, x_2, \ldots, x_n, \ldots$ with probability $p_1, p_2, \ldots, p_n, \ldots$
- Assume $\sum_i p_i = 1$, or normalize it
- Divide the interval [0,1) in n subintervals, with limits

$$y_0 = 0, \quad y_1 = p_1, \quad y_2 = p_1 + p_2, \ldots$$

- Generate a uniform pseudo-random number $\xi$
- Find the $i^{th}$ y-interval such that

$$y_{i-1} \le \xi < y_i$$

- Select $X = x_i$ as the sampled value




Since $\xi$ is uniformly random:

$$P(x_i) = P(y_{i-1} \le \xi < y_i) = y_i - y_{i-1} = p_i$$

# Sampling from a distribution – *Discrete*

2) By adjusting weights

- Suppose to have a fluence energy spectrum $\Phi$ given in N discrete energy bins between $E_0$ and $E_N$ : $\Phi_1,\ldots,\Phi_N$
- Generate a uniform pseudo-random number $\xi$
- Find the $i^{th}$ energy bin such that

$$E_{i-1} \leq \xi\,(E_N - E_0) < E_i$$

- Generate another uniform pseudo-random number $\xi \in [0,1)$ and sample an energy uniformly within the $i^{th}$ energy bin
- assign a weight $\Phi_i$ to that primary particle

***Note:*** This method is often used for spectra steeply decreasing with energy (e.g., $\Phi \sim 1/E$), where the result depends significantly on the particle cascades initiated by high energy primaries, as it ensures faster convergence to the true value.

# Example Sampling from a histogram - 1

```
      PARAMETER (NMAX=1000)
      DIMENSION ERG(NMAX), CUM(NMAX)
      CHARACTER*250 LINE
      SAVE  N, ERG, CUM

       IF ( LFIRST ) THEN
       …
            LUNRD = NINT(WHASOU(1))
            N = 0
            SUM   = ZERZER
            EPREV = ZERZER
 10         CONTINUE
              READ (LUNRD, '(A)', ERR=9999, END=20 ) LINE
              READ (LINE, *, ERR=10) E, H
              N = N + 1
              IF (N .GT. NMAX)
     &             CALL FLABRT('SOURCE','Please increase NMAX')
              IF (N .EQ. 1 .AND. ABS(H).GT.AZRZRZ)
     &             CALL FLABRT(
     &                  'SOURCE','ZERO was expected as first value')
*** Create cumulative sum of dE*V
              SUM = SUM + H*(E-EPREV)
              EPREV = E
              ERG(N) = E
              CUM(N) = SUM
          GO TO 10
 20       CONTINUE
          CLOSE (LUNRD)
      END IF
9999 CALL FLABRT('SOURCE', 'Error reading source file')
```

*Logical unit* from input file as WHAT(1) of the SOURCE card. Use OPEN card to open the file which contains *pairs Energy-Value*. First value is supposed to be 0 in order to set the *lower energy limit*.

Example: hsource.f

# Example Sampling from a histogram - 2

```
*  From this point .....

*** Select a random energy interval
      C = CUM(N) * FLRNDM(C)
*** Find interval (CUM(1)=0)
      DO I=2,N
        IF (CUM(I) .GT. C) THEN
***         Found interval I, select a random energy inside
            E = ERG(I-1) + (ERG(I)-ERG(I-1))*FLRNDM(C)
            GO TO 90
        END IF
      END DO
```

Select a random cumulative value

# Sampling from a distribution – *Continuous*

## 1) By integration

- Integrate the distribution function *f(x)*, analytically or numerically, and normalize to 1 to obtain the normalized cumulative distribution

$$F(x) = \frac{\int_{x_{\min}}^{x} f(t)dt}{\int_{x_{\min}}^{x_{\max}} f(t)dt}$$

- Generate a uniform pseudo-random number $\xi \in [0,1)$
- Get the desired result by finding the inverse value $x = F^{-1}(\xi)$, analytically or most often numerically, i.e. by interpolation (table look-up)

Since $\xi$ is uniformly random:

$$P(a < x < b) = P(F(a) \le \xi < F(b)) = F(b) - F(a) = \int_a^b f(x)dx$$

# Sampling from a distribution – *Continuous*

***Example***

Take $f(x) = e^{-\frac{x}{\lambda}}$, x ∈ [0,∞)

Cumulative distribution:

$$F(t) = \int_0^t e^{-\frac{x}{\lambda}} dx = \lambda \times \left(1 - e^{-\frac{t}{\lambda}}\right)$$

Normalized:

$$F'(t) = \int_0^t \frac{e^{-\frac{x}{\lambda}}}{\lambda} dx = 1 - e^{-\frac{t}{\lambda}}$$

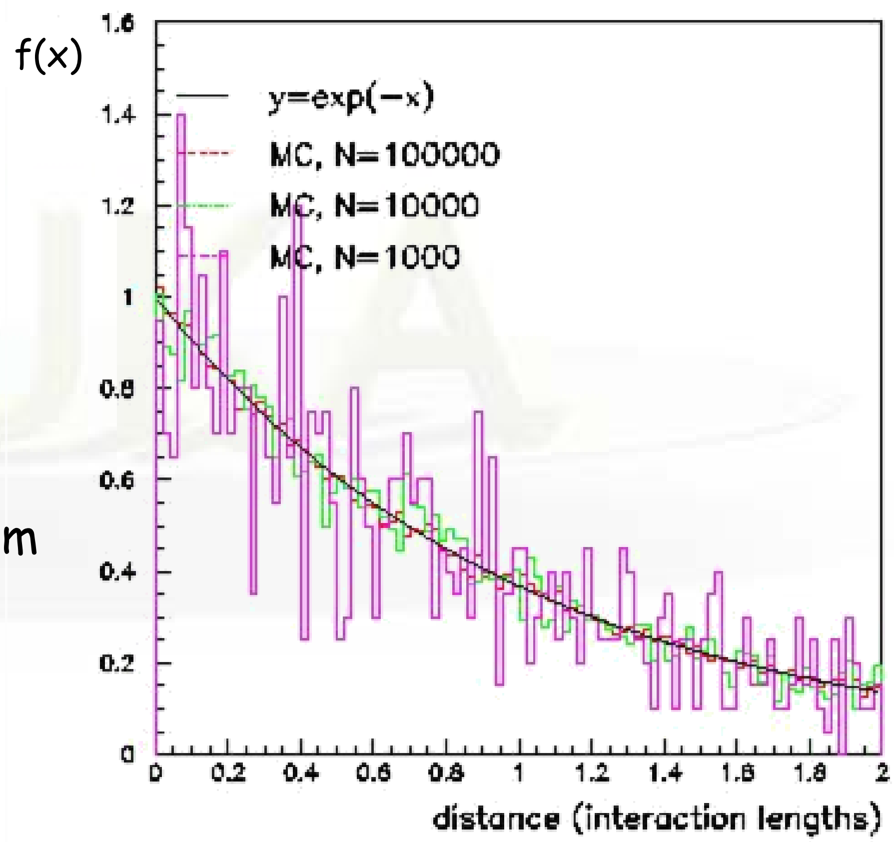
Generate a uniform pseudo-random number $\xi$ ∈ [0,1)

$$1 - e^{-\frac{t}{\lambda}} = \xi$$

Sample ***t*** by inverting

$$t = -\lambda \ln(1 - \xi)$$

Repeat N times



# Sampling from a distribution – *Continuous*

## 2) By rejection

- Let be *f′(x)*, a normalized distribution function, which cannot be sampled by integration and inversion
- Let be *g′(x)*, a normalized distribution function, which can be sampled, and such that $Cg'(x) \geq f'(x)$, $\forall\, x \in [x_{min}, x_{max}]$
- Sample X from g′(x), and generate a uniform pseudo-random number $\xi \in [0,1)$
- Accept X if $\xi < f'(X)/Cg'(X)$ , if not repeat the previous step

The overall efficiency (accepted/sampled) is given by:

$$R = \int \frac{f'(x)}{Cg'(x)} g'(x)\,dx = \frac{1}{C}$$

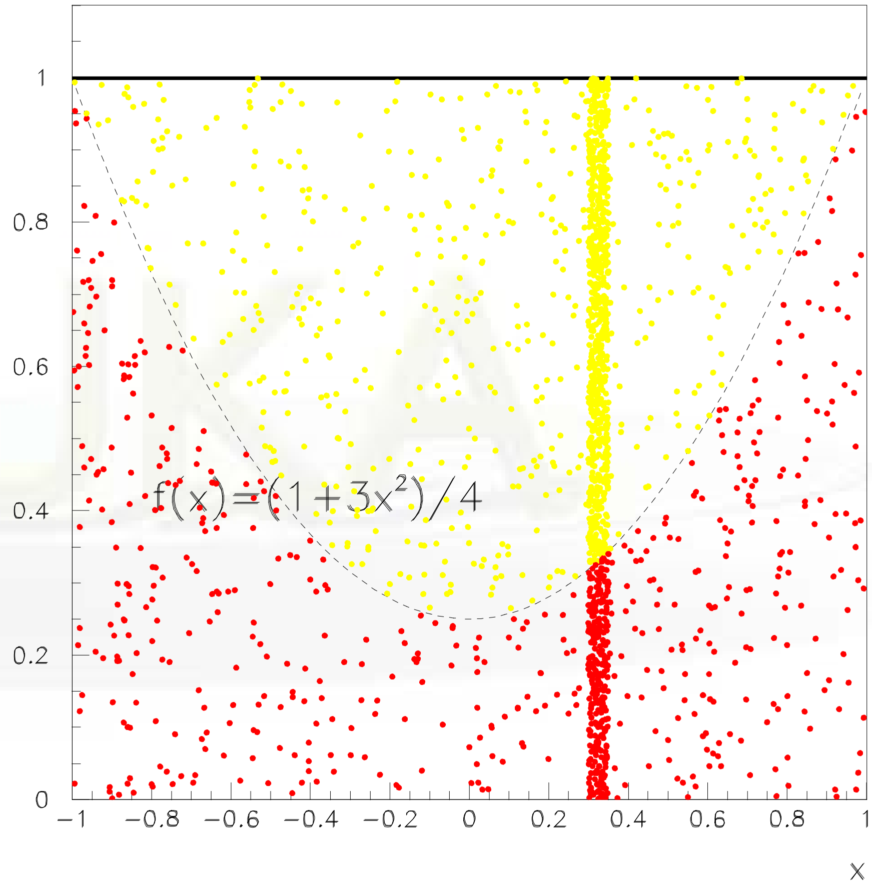
and the probability that X is accepted is unbiased:

$$P(X)\,dX = \frac{1}{R} g'(X)\,dX \times \frac{f'(X)}{Cg'(X)} = f'(X)\,dX$$

# Sampling from a distribution – *Continuous*

***Example***

- Let be $f'(x) = (1+3x^2)/4$, $x \in [-1,1]$,
- Take $g'(x)=1/2$, $C=2$
- Generate two uniform pseudo-random numbers $\xi_1, \xi_2 \in [0,1)$
- Accept $X=2\xi_1-1$ if $\xi_2 < (1+3X^2)/4$, if not repeat



# Sampling from a distribution – *Continuous*

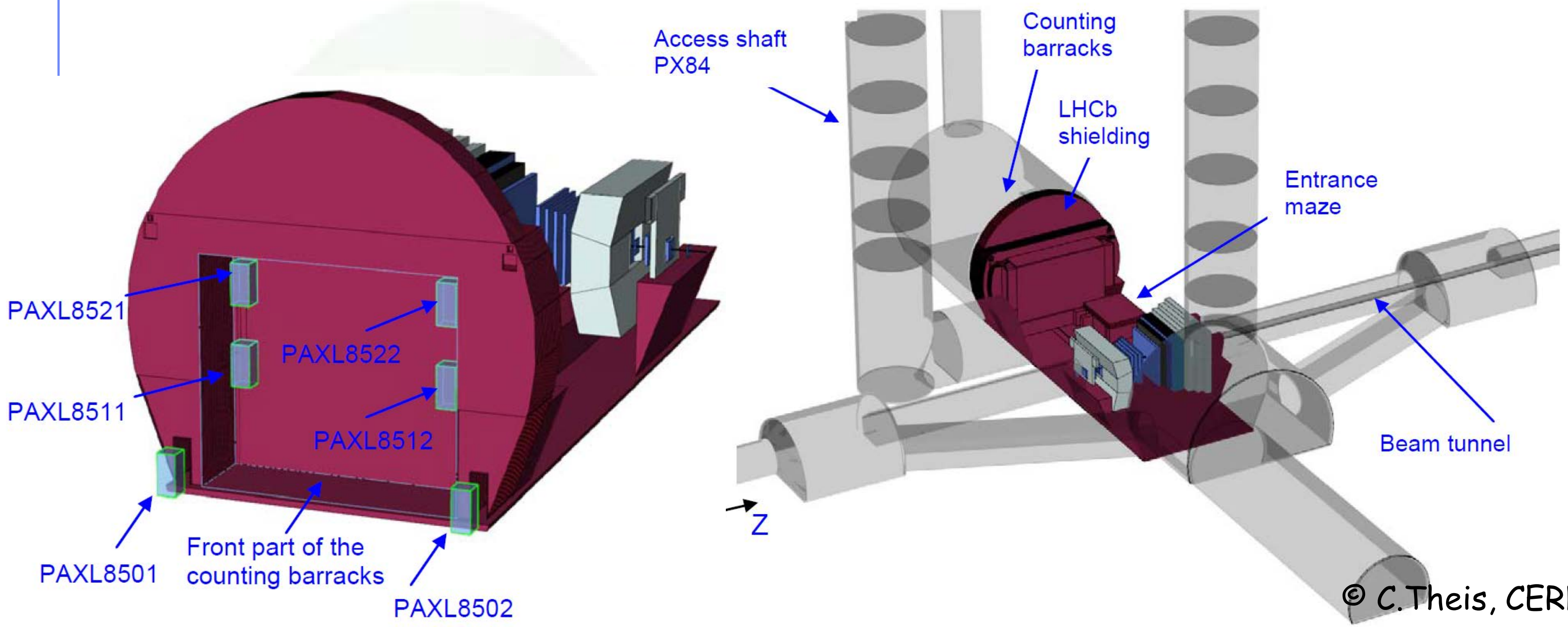
3) By adjusting weights

- Suppose to have a fluence energy spectrum $\Phi(E)$ given in between $E_0$ and $E_1$
- Generate a uniform pseudo-random number $\xi \in [0,1)$ and calculate the sampled energy $E = E_0 + \xi\,(E_1 - E_0)$
- Assign a weight $\Phi(E)$ to that primary particle

# Two-step methods

***Example:***

predict reading of a (small) radiation detector at a remote location in a huge geometry, *e.g.*, LHCb experiment at CERN




© C.Theis, CERN

Problem: direct calculation in one step highly inefficient due to the small affected phase-space

# Two-step methods

Solution: split simulation into two steps
1) Calculation of radiation field at detector location
2) Simulation of detector reading

**Two possibilities:**

*Directional dependence of detector reading is negligible*

- calculate **average fluence energy spectra**, separately for different particle types, at the detector location
- simulate reading of detector with user-defined source which reads in the calculated spectra and samples particle type, energy and direction (*e.g.*, isotropic incidence)
- ***important:*** results of the second step have to be **normalized to the integrated particle fluence** obtained in the first step

*Directional dependence of detector reading is important*

- replace detector by 'blackhole' and write all information on particles entering it (type, energy, position, direction) into an **external file**
- simulate reading of detector (if possible with the original geometry now containing the detector) with user-defined source which reads in the particles from the external file
- ***important:*** **pick entries randomly** from external file to avoid going through identical sequence of particles if several runs are performed

# Two-step example – Dumping particles

You can dump the particles with several ways e.g.:

- mgdraw.f activated with USERDUMP
- fluscw.f activated with USERWEIGht

The following example is using fluscw.f activated with USERWEIGht and coupled with the first USRBDX scoring

```
* Activate with USERWEIGht Use FLUSCW+ (WHAT(3)>2)
* Couple scoring with the first Boundary crossing estimator
      IF (ISCRNG.EQ.1 .AND. JSCRNG.EQ.1) THEN
               IF (LFIRST) THEN
                   WRITE (99,*)
     &  '# 1.IJ  2.X 3.Y 4.Z  5.TX 6.TY 7.TZ   8.E 9.W'
                   LFIRST = .FALSE.
               END IF
               WRITE (99,'(I3,8(1X,F22.14))')
     &                 IJ,XX,YY,ZZ,TXX,TYY,TZZ,-PLA,WEE
      END IF
```

Example: rdfluscw.f

# Two-step example – Sampling particles - 1

```
      PARAMETER (NMAX=1000000)
      SAVE LFIRST
      DATA LFIRST / .TRUE. /
      CHARACTER*250 LINE
      DIMENSION  IJ(NMAX)
      DIMENSION  XXX(NMAX), YYY(NMAX), ZZZ(NMAX)
      DIMENSION  UUU(NMAX), VVV(NMAX), WWW(NMAX)
      DIMENSION  ERG(NMAX), WGT(NMAX)
      SAVE IJ, XXX, YYY, ZZZ
      SAVE UUU, VVV, WWW
      SAVE ERG, WGT

      IF ( LFIRST ) THEN
         LUNRD = NINT(WHASOU(1))
         NNN = 0
 10      CONTINUE
            READ( LUNRD, '(A)', ERR=9999, END=20 ) LINE
            READ (LINE,*,ERR=10) I, X, Y, Z, U, V, W, E, WG
            NNN = NNN + 1
            IF (NNN.GT.NMAX) CALL FLABRT('SOURCE','Increase NMAX')
            …
```

*Logical unit* from input file as WHAT(1) of the SOURCE card. Use OPEN card to open the file

Example: rdsource.f

# Two-step example - Sampling particles - 2

```
            IJ(NNN)  = I
             XXX(NNN) = X
             YYY(NNN) = Y
             ZZZ(NNN) = Z
*  |  Normalize direction cosines to 1.0
             UVW = SQRT(U**2 + V**2 + W**2)
             UUU(NNN) = U / UVW
             VVV(NNN) = V / UVW
             WWW(NNN) = W / UVW
             ERG(NNN) = E
             WGT(NNN) = WG
          GOTO 10
 20       CONTINUE
          IF (NNN.EQ.0) CALL FLABRT('SOURCE','Error reading file')
          WRITE (LUNOUT,*)
          WRITE (LUNOUT,*) '*** rdsource: ',NNN,' particles loaded'
          WRITE (LUNOUT,*)
       END IF
```

Example: rdsource.f

# Two-step example – Sampling particles - 3

Choose a random particle
Results will be normalized per recorded particle

Push particle into stack

```
      RNDSIG = FLRNDM (RNDSIG)
      N = INT(NNN*RNDSIG)+1
* Wt is the weight of the particle
      WTFLK  (NPFLKA) = WGT(N)
      ILOFLK (NPFLKA) = IJ(N)

* Kinetic energy of the particle (GeV)
      TKEFLK (NPFLKA) = ERG(N)
* Particle momentum
      PMOFLK (NPFLKA) = SQRT ( TKEFLK (NPFLKA) * ( TKEFLK (NPFLKA)
     &                      + TWOTWO * AM (IONID) ) )
* Cosines
      TXFLK  (NPFLKA) = UUU(N)
      TYFLK  (NPFLKA) = VVV(N)
      TZFLK  (NPFLKA) = WWW(N)
* Particle coordinates
      XFLK   (NPFLKA) = XXX(N) !+ XBEAM
      YFLK   (NPFLKA) = YYY(N) !+ YBEAM
      ZFLK   (NPFLKA) = ZZZ(N) !+ ZBEAM
```

Example: rdsource.f

# Two-step: Normalization and Errors

- The dumped particles represent only a fraction of the full shower → therefore the second step consists only of a subset of the full simulation
- Thus the results of the second step should be multiplied (normalized) with the recorded weight of the first step

$$\text{Normalization} = \frac{\sum \text{weights of recorded particles}}{\sum \text{weights of source particles}}$$

WARNING:

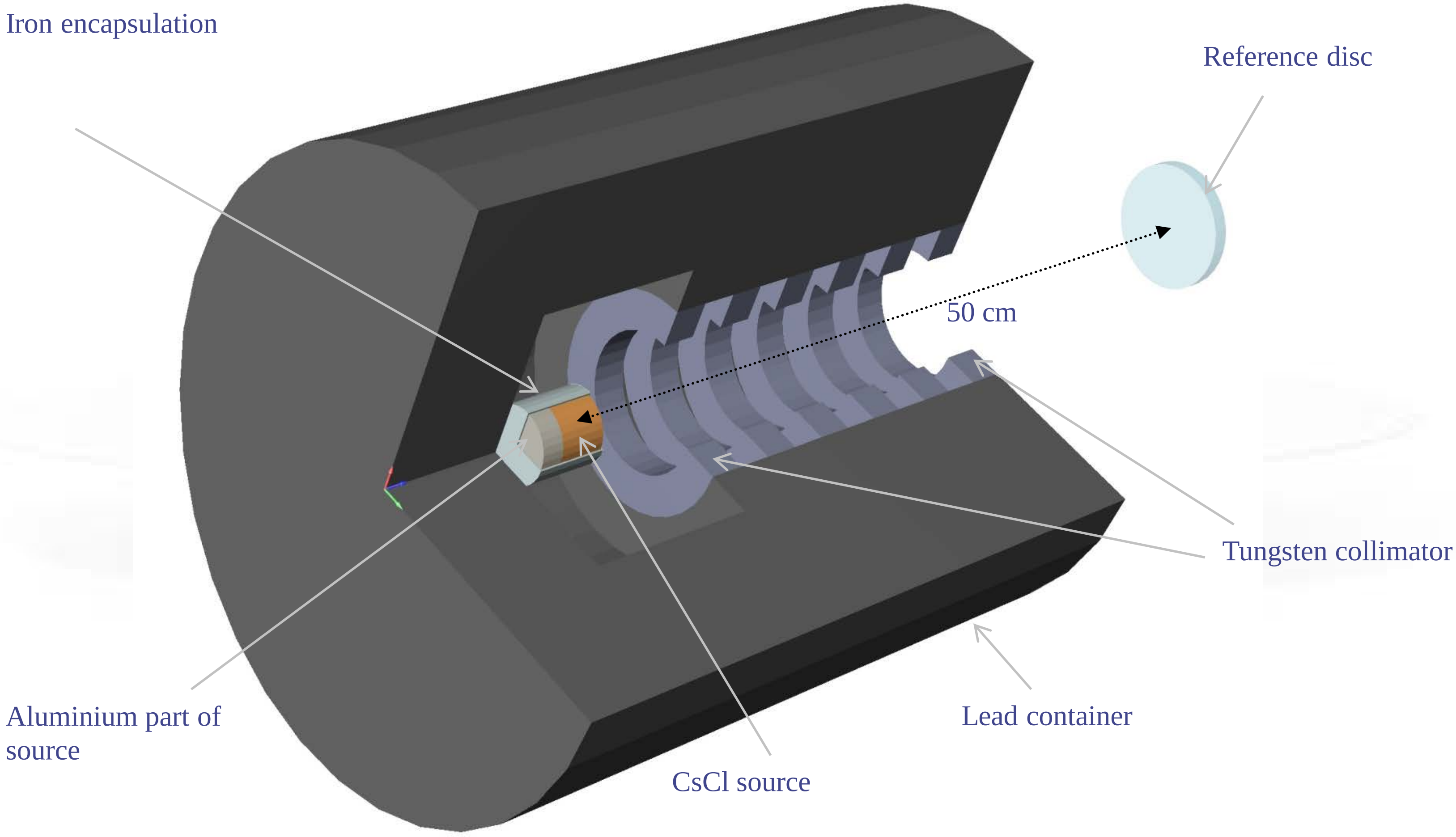
- verify that the recorded particles contains ALL the possible ones that contribute to the effect under study.
  You didn't miss any other that could have an impact on the results

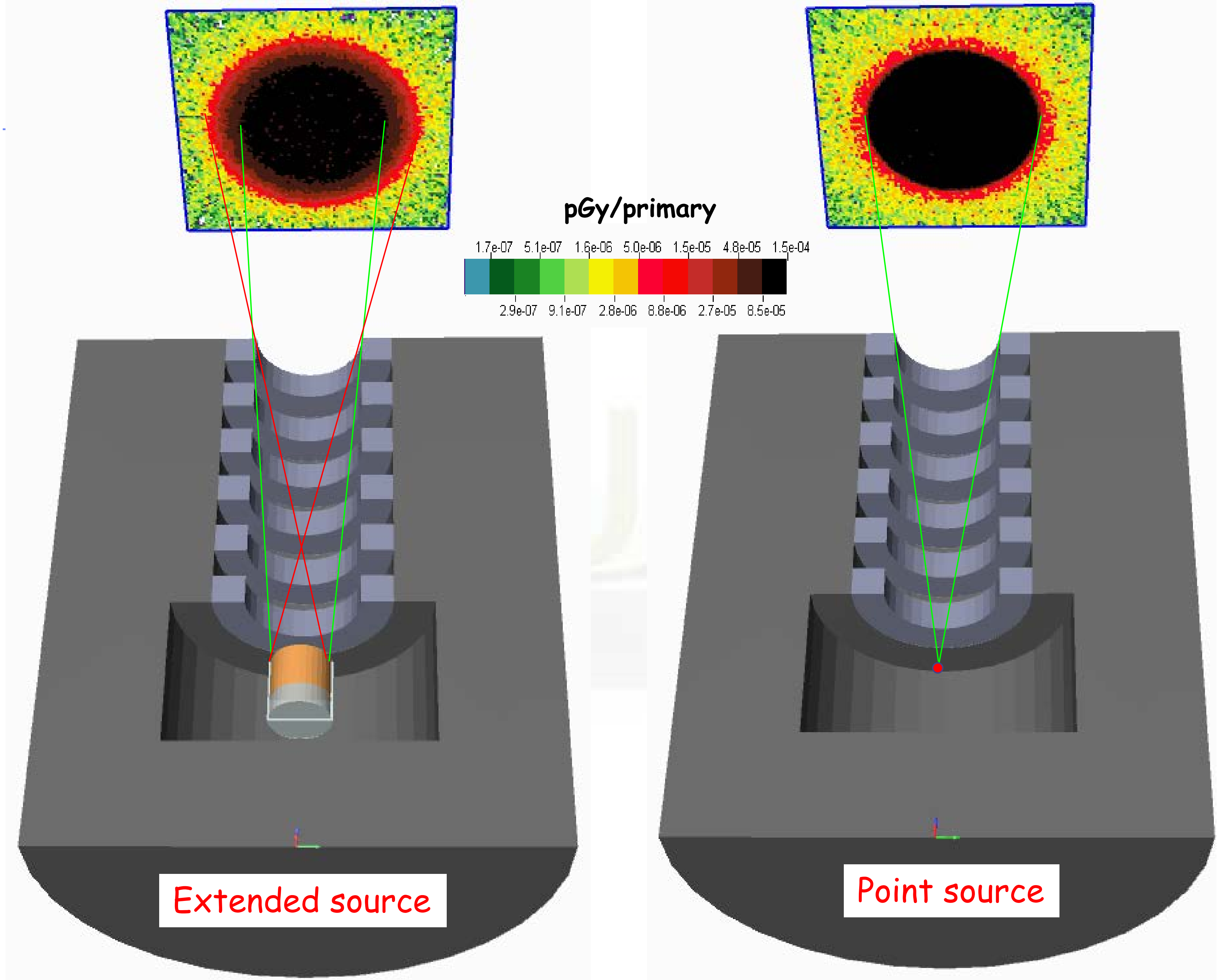
# Two-step: Things to remember

1. Sample randomly the recorded particles on the second step! It has many benefits: *i)* you don't have to go through the entire list sequentially (especially if enormous), *ii)* you can reuse particles, *iii)* immediate reproducibility of an aborted cycle
2. Verify your NORMALIZATION
   optionally you can make a full run to compare the results between the two step and full run
3. Like in a biasing run the purpose of a two step approach is to keep the mean but to reduce the error or time. Or to study different configurations.
4. *A* more honest two step approach will be to record several cycles (e.g. the typical 5 cycles) independently from the 1$^{st}$ step, and run separate 2$^{nd}$ steps one for each cycle.
   Merging the results will provide a more honest estimation of the variance
5. Verify that no other source of particles could contribute to your results (or at least is insignificant)

# Example:
point vs. extended source

# Example - *Cs irradiator*




pGy/primary
1.7e-07 5.1e-07 1.6e-06 5.0e-06 1.5e-05 4.8e-05 1.5e-04
2.9e-07 9.1e-07 2.8e-06 8.8e-06 2.7e-05 8.5e-05
Extended source
Point source

# Example - *Cs irradiator*