

## Summary

- Applications' View of a Relational Database Management System (RDBMS)
- Relational Algebra Overview
- SQL Overview
- Extended Relational Algebra/Equivalent SQL


## Applications' View of an RDBMS System

- Persistent data structure
- Large volume of data
- "Independent" from processes using the data
- High-level API for access \& modification
- Declarative, automatically optimized
- Transaction management (ACID)
- Atomicity: all or none happens, despite failures \& errors
- Concurrency
- Isolation: appearance of "one at a time"
- Durability: recovery from failures and other errors


## Data Structure: Relational Model

- Relational Databases: Schema + Data
- Schema:
- collection of tables
(also called relations)
- each table has a set of attributes
- no repeating relation names, no repeating attributes in one table
- Data (also called instance):
- set of tuples

| Movie |  |  |
| :--- | :--- | :--- |
| Title | Director | Actor |
| Wild | Lynch | Winger |
| Sky | Berto | Winger |
| Reds | Beatty | Beatty |
| Tango | Berto | Brando |
| Tango | Berto | Winger |
| Tango | Berto | Snyder |

- tuples have one value for each attribute of the table they belong



## Data Independence

- Physical Data Independence:

Applications are insulated from changes in physical storage details

## - Logical Data Independence:

Applications are insulated from changes to logical structure of the data

- Why are these properties important?
- Reduce program maintenance
- Logical database design changes over time
- Physical database design tuned for performance


## Summary

- Applications' View of a Relational Database Management System (RDBMS)
- Relational Algebra Overview
- SQL Overview
- Extended Relational Algebra/Equivalent SQL


## Basic Relational Algebra Operators

## - Selection ( $\sigma$ )

- $\sigma_{c} R$ selects tuples of the argument relation $R$ that satisfy the condition c
- The condition c consists of atomic predicates of the form
- attr = value
(attr is an attribute of $R$ )
- attr $_{1}=$ attr $_{2}$
- other operators possible

$$
\text { (e.g. }>,<,!=\text {, LIKE) }
$$

- Bigger conditions constructed by conjunctions (AND) and disjunctions (OR) of atomic predicates



## Basic Relational Algebra Operations

- Rename ( $\rho$ )
- $\rho_{\mathrm{A} \rightarrow \mathrm{B}} R$ renames attribute $A$ of relation $R$ into $B$
- $\rho_{S} R$ renames relation $R$ into $S$
- Union ( $\cup$ )
- applies to two tables $R$ and $S$ with same schema
$-R \cup S$ is the set of tuples that are in $R$ or $S$ or both
- Difference (-)
- applies to two tables $R$ and $S$ with same schema
- $R-S$ is the set of tuples in $R$ but not in $S$

Find all people, i.e., actors and directors, of the table Movie
$\pi_{\text {People }} \rho_{\text {Actor } \rightarrow \text { People }}$ Movie
$\cup \pi_{\text {People }} \rho_{\text {Director } \rightarrow \text { People }}$ Movie

Find all directors who are not actors
$\pi_{\text {Director }}$ Movie
$-\rho_{\text {Actor } \rightarrow \text { Director }} \pi_{\text {Actor }}$ Movie

## Other Relational Algebra Operations

- Extended Projection: Using the same $\pi_{\mathrm{L}} R$ operator, we allow the list $L$ to contain arbitrary expressions involving attributes

1. Arithmetic on attributes, e.g., $A+B \rightarrow C$
2. Duplicate occurrences of the same attribute

- Example



## Other Relational Algebra Operations

- Natural Join: R1 $\bowtie$ R2

A useful join variant connects two relations by:

- Equating attributes of the same name, and
- Projecting out one copy of each pair of equated attributes
- Example: Movie $\bowtie$ Schedule

| Title | Director | Actor | Theater |
| :---: | :---: | :---: | :---: |
| Wild | Lynch | Winger | Odeon |
| Sky | Berto | Winger | Forum |
| Reds | Beatty | Beatty | Forum |

## Other Relational Algebra Operations

- Theta-Join: R1 $凶_{C}$ R2
- Take the product R1 X R2
- Then apply $\sigma_{\mathrm{c}}$ to the result
- As for $\sigma$, c can be any boolean-valued condition
- Historic versions of this operator allowed only A $\theta$ B where $\theta$ is $=,<$, etc.; hence the name "theta-join"
- Example: Movie $\bigotimes_{\text {Movie.Title=Schedule.Title }}$ Schedule

| Movie.Title | Director | Actor | Schedule.Title | Theater |
| :---: | :---: | :---: | :---: | :---: |
| Wild | Lynch | Winger | Wild | Odeon |
| Sky | Berto | Winger | Sky | Forum |
| Reds | Beatty | Beatty | Reds | Forum |

## Building Complex Expressions

- Algebras allow us to express sequences of operations in a natural way
- Example: in arithmetic - $(x+4)^{*}(y-3)$
- Relational algebra allows the same
- Three notations, just as in arithmetic:

1. Sequences of assignment statements
2. Expressions with several operators
3. Expression trees

## Sequences of Assignments

- Create temporary relation names
- Renaming can be implied by giving relations a list of attributes
- Example: R3 := R1 $\bowtie_{C} \mathbf{R 2}$ can be written: R4: = R1 X R2
R3: $=\sigma_{\mathrm{c}}(\mathrm{R} 4)$


## Expression Trees

- Leaves are operands - either variables standing for relations or particular, constant relations
- Interior nodes are operators, applied to their child or children

$$
\begin{gathered}
\pi_{\text {s.Theater }} \\
\sigma_{\text {M.Title }=\text { s.Title AND M.Actor }=\text { ' Winger' }} \\
\text { Movie } \mathrm{M} \\
\quad \text { Schedule S }
\end{gathered}
$$

## Expressions in a Single Assignment

- Example: the theta-join $\mathbf{R 3} \mathbf{: =} \mathbf{R 1} \bowtie_{C} \mathbf{R} \mathbf{2}$ can be written: R3:= $\sigma_{\mathrm{c}} \mathbf{( R 1} \mathbf{X} \mathbf{R 2 )}$
- Precedence of relational operators:

1. Unary operators - select, project, rename - have highest precedence, bind first
2. Then come products and joins
3. Then intersection
4. Finally, union and set difference bind last

D But you can always insert parentheses to force the order you desire

## Schemas for Interior Nodes

- An expression tree defines a schema for the relation associated with each interior node
- Similarly, a sequence of assignments defines a schema for each relation on the left of the := sign


## Schema-Defining Rules 1

- For union, intersection, and difference, the schemas of the two operands must be the same, so use that schema for the result
- Selection: schema of the result is the same as the schema of the operand
- Projection: list of attributes tells us the schema


## Relational Algebra on Bags

- A bag is like a set, but an element may appear more than once
- Multiset is another name for "bag"
- Example:
- $\{1,2,1,3\}$ is a bag
- $\{1,2,3\}$ is also a bag that happens to be a set
- Bags also resemble lists, but order in a bag is unimportant
- Example: $\{1,2,1\}=\{1,1,2\}$ as bags, but $[1,2,1]!=[1,1,2]$ as lists


## Schema-Defining Rules 2

- Product: the schema is the attributes of both relations
- Use R.A, etc., to distinguish two attributes named $A$
- Theta-join: same as product
- Natural join: use attributes of both relations
- Shared attribute names are merged
- Renaming: the operator tells the schema


## Why Bags?

- SQL, the most important query language for relational databases is actually a bag language
- SQL will eliminate duplicates, but usually only if you ask it to do so explicitly
- Some operations, like projection, are much more efficient on bags than sets


## Operations on Bags

- Selection applies to each tuple, so its effect on bags is like its effect on sets
- Projection also applies to each tuple, but as a bag operator, we do not eliminate duplicates
- Products and joins are done on each pair of tuples, so duplicates in bags have no effect on how we operate



## Examples

- Bag Selection

$$
\sigma_{\mathrm{A}+\mathrm{B}<5}(R)=\begin{array}{|cc|}
\hline \mathrm{A} & \mathrm{~B} \\
\hline 1 & 2 \\
\hline 1 & 2 \\
\hline
\end{array}
$$



- Bag Projection



## Bag Union

- Union, intersection, and difference need new definitions for bags
- An element appears in the union of two bags the sum of the number of times it appears in each bag
- Example:
$\{1,2,1\} \cup\{1,1,2,3,1\}=\{1,1,1,1,1,2,2,3\}$


## Bag Intersection

- An element appears in the intersection of two bags the minimum of the number of times it appears in either
- Example: $\{1,2,1\} \cap\{1,2,3\}=\{1,2\}$


## Beware: Bag Laws != Set Laws

- Not all algebraic laws that hold for sets also hold for bags
- Example: the commutative law for union does hold for bags $(R \cup S=S \cup R)$
- Since addition is commutative, adding the number of times $x$ appears in $R$ and $S$ doesn't depend on the order of $R$ and $S$


## Bag Difference

- An element appears in the difference $A-B$ of bags as many times as it appears in $A$, minus the number of times it appears in $B$
- But never less than 0 times
- Example:

$$
\begin{aligned}
& \{1,2,1\}-\{1,2,3\}=\{1\} \\
& \{1,2,1\}-\{1,1,1\}=\{2\}
\end{aligned}
$$

## An Example of Inequivalence

- Set union is idempotent, meaning that $S \cup S=S$
- However, for bags, if $x$ appears $n$ times in $S$, then it appears $2 n$ times in $S \cup S$
- Thus $S \cup S!=S$ in general


## Summary

- Applications' View of a Relational Database Management System (RDBMS)
- Relational Algebra Overview
- SQL Overview
- Extended Relational Algebra/Equivalent SQL


## SQL Queries: Aliases

- Use the same relation more than once in the FROM clause
- Tuple variables
- Example: Find actors who are also directors

SELECT t.Actor
FROM Movie t, Movie s
WHERE t.Actor=s.Director

## SQL Queries: The Basic From

- Basic form

SELECT $a_{1}, \ldots, a_{N}$
FROM $R_{1}, \ldots, R_{M}$ [WHERE condition]

- Equivalent relational algebra expression
$\pi_{\mathrm{a}_{1}, \ldots, \mathrm{a}_{\mathrm{N}}} \sigma_{\text {condition }}\left(R_{1} \times \ldots \times R_{M}\right)$
- WHERE clause is optional
- When more than one relations in the FROM clause have an attribute named $A$, we refer to a specific $A$ attribute as <RelationName>.A

Find titles of currently playing movies
SELECT Title
FROM Schedule

Find the titles of all movies by "Berto"
SELECT Title
FROM Schedule
WHERE Director="Berto"
Find the titles and the directors of all currently playing movies

SELECT Movie.Title, Director FROM Movie, Schedule WHERE Movie.Title=Schedule.Title

## SQL Queries: Nesting

- The WHERE clause can contain predicates of the form

> - attr/value IN <query>

- attr/value NOT IN


## <query>

- The predicate is satisfied if the attr or value appears in the result of the nested <query>
- Queries involving nesting but no negation can always be un-nested, unlike queries with nesting and negation

Typical use: "Find objects that always satisfy property X, e.g., find actors playing in every movie by Berto"

SELECT Actor
FROM Movie
WHERE Actor NOT IN SELECT t.Actor
FROM Movie $t$, Movie s
WHERE s.Director="Berto
AND t.Actor NOT IN (
SELECT Actor FROM Movie WHERE Title=s.Title )
)

The shaded query finds actors NOT playing in some movie by "Berto". The top lines complement the shaded part.

## Homework Problem

- Compare with shaded subquery of previous slide. The sample data may help you.


## SELECT Actor <br> FROM Movie

WHERE Actor NOT IN (
SELECT Actor
FROM Movie
WHERE Director="Berto"

| Actor | Director | Movie |
| :---: | :---: | :---: |
| a | B | 1 |
| a | B | 2 |
| b | B | 1 |
| c | X | 3 |
| d | B | 1 |
| d | B | 2 |
| d | X | 3 |

Nested Queries:
Existential Quantification

- A op ANY <nested query> is satisfied if there is a value $X$ in the result of the <nested query> and the condition $A$ op $X$ is satisfied
- (= ANY) $\equiv \mathbf{I N}$
- But, ( $\neq$ ANY) $\neq$ NOT IN

Find directors of currently playing movies

SELECT Directo FROM Movie
WHERE Title = ANY
SELECT Title
FROM Schedule


## Nested Queries: Set Comparison

<nested query 1 > CONTAINS
<nested query 2>
ind actors playing in every movie by "Berto"

SELECT s.Actor
FROM Movie s WHERE
(SELECT Title
FROM Movie
WHERE t.Actor $=\mathrm{s}$.Actor
CONTAINS
(SELECT Title
FROM Movie
WHERE Director = "Berto")

## SQL: Union, Intersection, Difference

- Union
<SQL query 1 > UNION
<SQL query 2>
- Intersection
<SQL query $1>$ INTERSECT
<SQL query 2>
- Difference
<SQL query 1> MINUS
<SQL query 2>

Find all actors or directors
(SELECT Actor
FROM Movie)
UNION
(SELECT Director
FROM Movie)

Find all actors who are not directors
(SELECT Actor
FROM Movie)
MINUS
(SELECT Director FROM Movie)

## NULL Values

- Tuples in SQL relations can have NULL as a value for one or more components
- Meaning depends on context. Two common cases:
- Missing value: e.g., we know movie Tango has a third actor, but we don't know who she/he is

| Title | Director | Actor |
| :---: | :---: | :---: |
| Tango | Berto | Brando |
| Tango | Berto | Winger |
| Tango | Berto | NULL |

- Inapplicable: e.g., the value of attribute spouse for an unmarried person


## Comparing NULL's to Values

- The logic of conditions in SQL is really 3 -valued logic: TRUE, FALSE, UNKNOWN
- Comparing any value (including NULL itself) with NULL yields UNKNOWN
- A tuple is in a query answer iff the WHERE clause is TRUE (not FALSE or UNKNOWN)

To understand how AND, OR, and NOT work in 3 -valued logic, think of TRUE $=1$, FALSE $=0$, and UNKNOWN = 1⁄2

- $\operatorname{AND}=$ MIN; OR $=$ MAX, $\operatorname{NOT}(x)=1-x$
- Example:

TRUE AND (FALSE OR NOT(UNKNOWN)) = $\operatorname{MIN}(1, \operatorname{MAX}(0,(1-1 / 2)))=$
$\operatorname{MIN}(1, \operatorname{MAX}(0,1 / 2))=\operatorname{MIN}(1,1 / 2)=1 / 2$

## Surprising Example

- From the following Sells relation:

| book | store | price |
| :---: | :---: | :---: |
| Harry Potter | Amazon | NULL |

SELECT book
FROM Sells
WHERE $\underset{\text { UNKNOWN }}{\rightleftarrows}$ price 20.00 OR price >= 20.00;


## Bag Semantics

- Although the SELECT-FROM-WHERE statement uses bag semantics, the default for union, intersection, and difference is set semantics
- That is, duplicates are eliminated as the operation is applied


## Reason:

## 2-Valued Laws != 3-Valued Laws

- Some common laws, like commutativity of AND, hold in 3-valued logic
- But not others, e.g., the law of the excluded middle: $p$ OR NOT $p=$ TRUE
- When $p=$ UNKNOWN, the left side is

$$
\operatorname{MAX}(1 / 2,(1-1 / 2))=1 / 2!=1
$$

## Motivation: Efficiency

- When doing projection, it is easier to avoid eliminating duplicates
- Just work tuple-at-a-time
- For intersection or difference, it is most efficient to sort the relations first
- At that point you may as well eliminate the duplicates anyway



## Summary

- Applications' View of a Relational Database Management System (RDBMS)
- Relational Algebra Overview
- SQL Overview
- Extended Relational Algebra/Equivalent SQL

| The Extended Algebra |
| :---: |
| $\delta=$ eliminate duplicates from |
| T = sort tuples |
| $Y=$ grouping and aggregation |

## Duplicate Elimination

- R1 := $\delta_{\text {(R2) }}$
- R1 consists of one copy of each tuple that appears in R2 one or more times
$\gamma=$ grouping and aggregation
- Example:


$\delta(\mathrm{R})=$|  | A |
| :---: | :---: |
|  | $B$ |
|  | 3 |

## Sorting

- R1: $=T_{L}(R 2)$
- $L$ is a list of some of the attributes of R2
- R1 is the list of tuples of R2 sorted first on the value of the first attribute on $L$, then on the second attribute of $L$, and so on
- Break ties arbitrarily

T is the only operator whose result is neither a set nor a bag

## Aggregation Operators

- Aggregation operators are not operators of relational algebra
- Rather, they apply to entire columns of a table and produce a single result
- The most important examples: SUM, AVG, COUNT, MIN, and MAX
- Example: R

$\operatorname{SUM}(\mathrm{A})=7$
$\operatorname{COUNT}(A)=3$
$\operatorname{MAX}(B)=4$
$\operatorname{AVG}(B)=3$


## Grouping Operator

- R1: $=\gamma_{L}$ (R2)
$L$ is a list of elements that are either:

1. Individual (grouping) attributes
2. AGG(A), where AGG is one of the aggregation operators and $A$ is an attribute

- An arrow and a new attribute name renames the component


## Applying $Y_{L}(R)$

- Group $R$ according to all the grouping attributes on list $L$
- That is: form one group for each distinct list of values for those attributes in $R$
- Within each group, compute $\operatorname{AGG}(A)$ for each aggregation on list $L$
- Result has one tuple for each group:

1. The grouping attributes and
2. Their group's aggregations


## Outerjoin

- Suppose we join $R \bowtie_{C} S$
- A tuple of $R$ that has no tuple of $S$ with which it joins is said to be dangling - Similarly for a tuple of $S$
- Outerjoin preserves dangling tuples by padding them with NULLs



## SQL Outerjoins

- R OUTER JOIN S is the core of an outerjoin expression
- It is modified by:

1. Optional NATURAL in front of OUTER $\longleftarrow$ Only one
2. Optional ON <condition> after JOIN $\square$ of these
3. Optional LEFT, RIGHT, or FULL before OUTER

- LEFT = pad dangling tuples of R only
- RIGHT = pad dangling tuples of S only
- FULL = pad both; this choice is the default


## SQL Aggregations

- SUM, AVG, COUNT, MIN, and MAX can be applied to a column in a SELECT clause to produce that aggregation on the column
- Also, COUNT(*) counts the number of tuples
- Example: Find the average salary of all employees


SELECT AvgSal = AVG(Salary) FROM Employee

Eliminating Duplicates in a SQL Accrecation

- Use DISTINCT inside an aggregation
- Example: Find the number of different departments:

SELECT COUNT(DISTINCT Dept)
FROM Employee

| Employee |  |  |
| :--- | :--- | :--- |
| Name | Dept | Salary |
| Joe | Toys | 45 |
| Nick | PCs | 50 |
| Jim | Toys | 35 |
| Jack | PCs | 40 |

## Example: Effect of NULL's

| SELECT COUNT(*) |
| :--- |
| FROM Employee <br> WHERE Dept="Toys"; |
| The number of employees <br> in the Toys department |
| SELECT COUNT(Salary) <br> FROM Employee <br> WHERE Dept="Toys";$\quad$The number of employees <br> in the Toys department |
| with a known salary |

WHERE Dept="Toys";

## SQL Grouping

- We may follow a SELECT-FROM-WHERE expression by GROUP BY and a list of attributes
- The relation that results from the SELECT-FROMWHERE is grouped according to the values of all those attributes, and any aggregation is applied only within each group


## Example: Null Values and Aggregates

- Example:

select count(a), count(b), avg(b), count(*) from $R$
group by a



## Example: SQL Grouping

Find the average salary for each department: SELECT Dept, AvgSal = AVG(Salary) FROM Employee GROUP BY Dept


| Employee |  |  |
| :---: | :---: | :---: |
| Name | Dept | Salary |
| Joe | Toys | 45 |
| Nick | PCs | 50 |
| Jim | Toys | 35 |
| Jack | PCs | 40 |

## Restriction on SELECT Lists With Acgrecation

- If any aggregation is used, then each element of the SELECT list must be either:

1. Aggregated, or
2. An attribute on the GROUP BY list

- Example: You might think you could find the department with the highest salary by:

SELECT Dept, MaxSal = MAX(Salary)
FROM Employee
But this query is illegal in SQL

## SQL HAVING Clauses

- HAVING <condition> may follow a GROUP BY clause
- If so, the condition applies to each group, and groups not satisfying the condition are eliminated


## Example: SQL HAVING

- Example: Find the average salary of for each department that has either more than 1 employee or starts with a "To":

SELECT Dept, AvgSal=(AVG(Salary))
FROM Employee
GROUP BY Dept
HAVING COUNT(Name) > 1 OR Dept LIKE "To"

## Requirements on HAVING Conditions

- Conditions may refer to attributes only if they are either:

1. A grouping attribute, or
2. Aggregated
(same condition as for SELECT clauses with aggregation)

## Summary of SQL Queries

- A query in SQL can consist of up to six clauses, but only the first two, SELECT and FROM, are mandatory.
- The clauses are specified in the following order:

```
SELECT <attribute list>
FROM <table list>
[WHERE <condition>]
[GROUP BY <grouping attribute(s)>]
[HAVING <group condition>]
[ORDER BY <attribute list>]
```


## Summary of SQL Queries (cont'd)

- The SELECT-clause lists the attributes or functions to be retrieved
- The FROM-clause specifies all relations (or aliases) needed in the query but not those needed in nested queries
- The WHERE-clause specifies the conditions for selection and join of tuples from the relations specified in the FROM-clause
- GROUP BY specifies grouping attributes
- HAVING specifies a condition for selection of groups
- ORDER BY specifies an order for displaying the result of a query
- A query is evaluated by first applying the WHERE-clause, then GROUP BY and HAVING, and finally the SELECTclause


## Recursion in SQL

- SQL:1999 permits recursive queries
- Example: find all employee-manager pairs, where the employee reports to the manager directly or indirectly (that is manager's manager, manager's manager's manager, etc.)

WITH RECURSIVE empl(employee_name, manager_name) AS ( SELECT employee_name, manager_name
FROM manager
UNION
SELECT manager.employee_name, empl.manager_name FROM manager, empl
WHERE manager.manager_name = empl.employe_name) SELECT *
FROM empl

- This example query computes the transitive closure of the manager relation


## The Power of Recursion

- Recursive queries make it possible to write queries, such as transitive closure queries, that cannot be written without recursion or iteration
- Intuition: Without recursion, a non-recursive noniterative program can perform only a fixed number of joins of manager with itself
- This can give only a fixed number of levels of managers
- Given a program we can construct a database with a greater number of levels of managers on which the program will not work

Computing transitive closure

- The next slide shows a manager relation and finds all employees managed by "Jones"
- Each step of the iterative process constructs an extended version of empl from its recursive definition
- The final result is called the fixed point of the recursive definition



## The Power of Recursion (cont'd)

- Recursive queries are required to be monotonic, that is, if we add tuples to manager the query result contains all of the tuples it contained before, plus possibly more
- Example:

SELECT AvgSal = AVG(Salary)
FROM Employee
is not monotone in Employee

- Inserting a tuple into Employee usually changes the average salary and thus deletes the old average salary

SQL as a Data Manipulation Language: Insertions

Inserting tuples INSERT INTO R $\operatorname{VALUES}\left(\mathrm{v}_{1}, \ldots, \mathrm{v}_{\mathrm{k}}\right)$;

- some values may be left NULL
- use results of queries for
insertion
INSERT INTO R
SELECT ...
FROM .
WHERE ..

INSERT INTO Movie VALUES ("Brave", "Gibson", "Gibson");

INSERT INTO Movie(Title,Director) VALUES ("Brave", "Gibson");

INSERT INTO EuroMovie SELECT *
FROM Movie
WHERE Director = "Berto"

SQL as a Data Manipulation Language: Deletions

- Deletion basic form: delete every tuple that satisfies <cond>
DELETE FROM $R$
WHERE <cond>

Delete the movies that are not currently playing
DELETE FROM Movie
WHERE Title NOT IN
SELECT Title
FROM Schedule


## This Time

- Relational Algebra
- Chapter 2: 2.4
- Chapter 5: 5.1, 5.2
- SQL
- Chapter 6
- Chapter 10: 10.2

